

## Original papers

## Empirical and learning machine approaches to estimating reference evapotranspiration based on temperature data



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## ABSTRACT

The precise estimation of reference evapotranspiration ( $ET_0$ ) is crucial for the planning and management of water resources and agricultural production. In this study, the applicability of the Hargreaves Samani (HS), artificial neural network (ANN), multiple linear regression (MLR) and extreme learning machine (ELM) models were evaluated to estimate  $ET_0$  based on temperature data from the Verde Grande River basin, southeastern Brazil. These models were evaluated in two scenarios: local and pooled. In the local scenario, training, calibration and validation of the models were performed separately at each station. In the pooled scenario, meteorological data from all stations were grouped for training and calibration and then separately tested at each station. The  $ET_0$  values estimated by the Penman-Monteith model (FAO-56 PM) were considered the target data. All the developed models were evaluated by cluster analysis and the following performance indices: relative root mean square error (RRMSE), Pearson correlation coefficient ( $r$ ) and Nash-Sutcliffe coefficient (NS). In both scenarios evaluated, local and pooled, the results revealed the superiority of the artificial intelligence methods (ANN and ELM) and the MLR model compared to the original and adjusted HS models. In the local scenario, the ANN (with  $r$  of 0.751, NS of 0.687 and RRMSE of 0.112), ELM (with  $r$  of 0.747, NS of 0.672 and RRMSE of 0.116) and MLR (with  $r$  of 0.743, NS of 0.665 and RRMSE of 0.068) models presented the best performance, in addition to being grouped in the same cluster. Similar to the observations from the local scenario, the ANN (with  $r$  of 0.718, NS of 0.555 and RRMSE of 0.165), ELM (with  $r$  of 0.724, NS of 0.601 and RRMSE of 0.151) and MLR (with  $r$  of 0.731, NS of 0.550 and RRMSE of 0.091) models presented the best performance in the pooled scenario and were grouped in the same cluster. The locally trained models presented higher precision than the models generated with pooled data; however, the models generated in the pooled scenario could be used to estimate  $ET_0$  in cases of unavailability of local meteorological data. Although the MLR, ANN and ELM models, based on temperature data, are appropriate alternatives to accurately estimate  $ET_0$  in the Verde Grande River basin, southeastern Brazil, the MLR model presents the advantage of the use of explicit algebraic equations, facilitating its application.

### 1. Introduction

The reference evapotranspiration ( $ET_0$ ), introduced by the Food and Agriculture Organization of the United Nations (FAO) as a methodology for computing crop evapotranspiration (Doorenbos and Pruitt, 1977), is an essential component in irrigation planning, river basin hydrology, and hydrological balance studies (Antonopoulos and Antonopoulos, 2017; Traore et al., 2010). In addition,  $ET_0$  is a key element in executing effective water management practices and optimizing their use in agricultural production areas (Smith, 2000). In the case of arid and

semi-arid regions, understanding  $ET_0$  is even more important for efficient irrigation planning (Huo et al., 2012).

$ET_0$  can be determined by lysimeters (Anapalli et al., 2016; Xu et al., 2018), the energy balance (Yan et al., 2017), scintillometers (Valayamkunnath et al., 2018), or by using empirical equations based on meteorological data (Antonopoulos and Antonopoulos, 2017). The Penman-Monteith (PM) method is universally recommended by the FAO as the only precise equation to calculate  $ET_0$  (Allen et al., 1998). The PM model incorporates thermodynamic and aerodynamic aspects, and it has been shown to be relatively accurate in humid and arid

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**Table 1**  
Meteorological stations and statistical properties of the meteorological variables of the study area.

Station (longitude; latitude and altitude)	Station code	Variable	Min	Max	Mean	SD	CV (%)
Espinosa (42.8°W, 14.9°S and 569.6 m)	1	Pr (mm)	0.0	126.7	1.9	7.7	411.2
		RH (%)	22.5	97.7	63.4	13.7	21.6
		Tmin (°C)	9.6	27.7	20.0	2.6	13.0
		Tmax (°C)	20.2	40.3	31.3	2.8	8.9
		U <sub>2</sub> (m s <sup>-1</sup> )	0.0	6.4	2.2	1.1	49.3
		Rs (MJ m <sup>-2</sup> )	7.5	76.6	21.9	4.9	22.3
		ET <sub>0</sub> (mm d <sup>-1</sup> )	1.5	11.5	4.9	1.3	26.3
Janaúba (43.3°W, 15.8°S and 516.0 m)	2	Pr (mm)	0.0	157.0	2.0	8.1	402.5
		RH (%)	21.0	97.8	59.1	13.9	23.6
		Tmin (°C)	7.8	29.0	19.3	2.5	13.0
		Tmax (°C)	20.2	41.8	32.1	2.9	9.1
		U <sub>2</sub> (m s <sup>-1</sup> )	0.0	7.5	1.1	1.0	94.9
		Rs (MJ m <sup>-2</sup> )	7.3	36.5	21.4	4.5	20.8
		ET <sub>0</sub> (mm d <sup>-1</sup> )	1.6	10.0	4.3	1.1	24.6
Juramento (43.7°W, 16.8°S and 650.0 m)	3	Pr (mm)	0.0	127.0	2.4	8.5	348.2
		RH (%)	24.0	99.8	69.6	12.5	17.9
		Tmin (°C)	4.2	25.3	16.8	3.2	19.3
		Tmax (°C)	19.7	40.0	29.9	2.8	9.5
		U <sub>2</sub> (m s <sup>-1</sup> )	0.0	6.5	1.1	0.5	45.1
		Rs (MJ m <sup>-2</sup> )	7.0	29.9	20.6	4.6	22.5
		ET <sub>0</sub> (mm d <sup>-1</sup> )	1.3	7.8	3.9	1.0	25.0
Montes Claros (43.8 °W, 16.7 °S and 646.3 m)	4	Pr (mm)	0.0	145.0	2.7	9.3	344.0
		RH (%)	24.0	98.3	62.7	14.6	23.4
		Tmin (°C)	5.8	28.0	18.0	3.0	16.4
		Tmax (°C)	20.0	40.3	30.2	2.9	9.5
		U <sub>2</sub> (m s <sup>-1</sup> )	0.0	4.0	1.4	0.5	33.5
		Rs (MJ m <sup>-2</sup> )	7.1	30.1	20.9	5.0	24.0
		ET <sub>0</sub> (mm d <sup>-1</sup> )	1.4	8.5	4.2	1.1	26.3
Monte Azul (42.8 °W; 15.1 °S and 603.6 m)	5	Pr (mm)	0.0	140.1	2.1	7.8	381.3
		RH (%)	21.0	98.8	58.6	14.3	24.4
		Tmin (°C)	11.3	28.0	20.4	2.2	11.0
		Tmax (°C)	20.7	41.1	31.3	2.9	9.2
		U <sub>2</sub> (m s <sup>-1</sup> )	0.0	6.7	1.7	1.1	60.3
		Rs (MJ m <sup>-2</sup> )	6.4	29.7	21.4	4.6	21.5
		ET <sub>0</sub> (mm d <sup>-1</sup> )	1.4	9.4	4.8	1.2	24.9

Pr – precipitation; RH – relative humidity; Tmin – minimum temperature; Tmax – maximum temperature; U<sub>2</sub> – wind speed; Rs – solar radiation; ET<sub>0</sub> – reference evapotranspiration by Penman-Monteith (Allen et al., 1998); Min – minimum; Max – maximum; SD – standard deviation; CV (%) – coefficient of variation.

regions (Smith et al., 1991; Yin et al., 2008). However, the greatest disadvantage of the PM method is the need for several types of climatic data that are not always available (Cobaner et al., 2017; Fan et al., 2018; Feng et al., 2017; Gocic et al., 2015).

In the Brazilian semi-arid region, the distribution and density of the meteorological stations are inadequate or insufficient, limiting the use of the PM method in irrigation management in this region, which has the largest public irrigated perimeter in Latin America and other important irrigation perimeters.

The Hargreaves Samani (HS) method is an alternative to the PM equation when the data set required by the PM model is not fully available (Allen et al., 1998; Cobaner et al., 2017). As shown by Almorox et al. (2015), the HS equation shows a more accurate performance in arid, semi-arid, temperate, cold and polar regions compared to other empirical models that rely on air temperature data to estimate ET<sub>0</sub>. However, this model overestimates ET<sub>0</sub> under high relative humidity conditions and underestimates it under conditions where the wind speed is higher than 3 m s<sup>-1</sup> (Allen et al., 1998; Didari and Ahmadi, 2019; Droogers and Allen, 2002). In this situation, the local calibration of empirical models or the creation of local equations is necessary.

In recent years, artificial intelligence (AI) methods, or soft computing methods, have been successfully applied to estimate and predict ET<sub>0</sub> in limited weather data situations. Artificial neural networks (ANNs) (Antonopoulos and Antonopoulos, 2017; Kumar et al., 2002; Traore et al., 2016; Traore et al., 2010), adaptive neuro-fuzzy inference systems (ANFIS) (Citakoglu et al., 2014; Dou and Yang, 2018), genetic programming (GP) (Kisi et al., 2015; Kisi and Sanikhani, 2015), support

vector machines (SVM), wavelet neural networks (Cobaner, 2013; Gocic et al., 2015; Fan et al., 2018; Kisi and Cimen, 2009), tree-based ensemble algorithms (i.e., random forest (RF), M5 model tree (M5Tree), gradient boosting decision tree (GBDT) and extreme gradient boosting (XGBoost)) (Fan et al., 2018; Feng et al., 2017a), generalized regression neural networks (GRNN) (Feng et al., 2017a) and extreme learning machines (ELM) (Dou and Yang, 2018; Feng et al., 2017b; Gocic et al., 2016) are examples of proposed AI models for the successful estimation of ET<sub>0</sub> in regions with low availability of meteorological data.

The Verde Grande River basin is one of the main irrigated fruit growing regions in Brazil and stands out because it has the largest irrigated perimeter in Latin America; however, the low availability of meteorological stations in the region hampers the accurate estimation of ET<sub>0</sub>. The development of improved methods to estimate the amount of water required by the crops is essential to improve the accuracy of the irrigation level and to increase the efficiency of water use (Antonopoulos and Antonopoulos, 2017), especially in areas with water scarcity problems, such as the semi-arid region, where the Verde Grande River basin is located. The low spatial density of meteorological stations in the Verde Grande River basin and its poor distribution make it impossible to apply the PM equation in irrigation management in most of the properties. Estimating calibrated models for the determination of ET<sub>0</sub> in the Verde Grande River basin using only temperature data can result in advances in irrigation management and regional hydrological studies, as well as a more economical alternative to the installation of new, spatially close meteorological stations.

The main objective of this study was to evaluate the applicability of different methods in estimating daily reference evapotranspiration

( $ET_0$ ) only with air temperature data as the input, thus allowing the accurate determination of  $ET_0$  in locations without available relative air humidity, solar radiation and wind speed data. To achieve this purpose, Hargreaves Samani (HS), adjusted HS, artificial neural network “multilayer perceptron” (ANN), multiple linear regression (MLR) and extreme learning machine (ELM) were compared to the Penman-Monteith method (FAO 56 – PM). These models were evaluated in two scenarios: local and pooled. In the local scenario, all models were trained, calibrated and validated separately at each station. In the pooled scenario, the meteorological data from all stations were grouped for training and calibration of the models and then tested separately at each station. The generation of models by a combined approach allows the estimation of  $ET_0$  in cases of unavailability of local meteorological data, that is, in regions that are distant from meteorological stations, but with the availability of temperature data.

## 2. Material and methods

### 2.1. Study area and data set

The Verde Grande River basin has an area of approximately 31,410 km<sup>2</sup> and a population of 741,500 inhabitants. The Verde Grande River basin stands out in the world scenario for housing the largest irrigated perimeter in Latin America, with the irrigation projects Jaíba, Gorutuba, Lagoa Grande and Estreito, and an irrigated area of approximately 742 km<sup>2</sup>. The study area is located in the semi-arid region of Brazil. The climate of the region is classified, according to Köppen, as Aw, warm tropical with a dry winter. The meteorological stations and statistical properties of the climatic variables are shown in Table 1.

The daily meteorological variables (maximum (Tmax) and minimum (Tmin) air temperature at a height of 2 m, mean relative humidity (RH), wind speed at a height of 10 m ( $U_{10}$ ) and sunshine duration) were obtained from the five meteorological stations of the Instituto Nacional de Meteorologia (INMET) located within the Verde

Grande River basin (Fig. 1) between 1996 and 2016. The meteorological data provided by INMET are of satisfactory quality certified by ISO 9001: 2008. (INMET, 2019). The missing data for Tmax and Tmin were reconstituted by the linear interpolation method, and the missing data for RH,  $U_2$  and  $R_s$  were estimated according to the methodology proposed by Allen et al. (1998).

### 2.2. FAO-56. Penman-Monteith model

The FAO-recommended Penman-Monteith equation (FAO 56-PM) (Equation (1)) (Allen et al., 1998) was used to estimate  $ET_0$  data, which were used as the targets for the calibration and evaluation of the HS, adjusted HS, MLR, ANN and, ELM models. This process is an accepted and commonly used practice (Antonopoulos and Antonopoulos, 2017; Didari and Ahmadi, 2019; Dou and Yang, 2018).

$$ET_0 = \frac{0.408\Delta(Rn - G) + \gamma \frac{900}{T+273} u_2 (e_s - e_a)}{\Delta + \gamma(1 + 0.34u_2)} \quad (1)$$

where  $ET_0$  is the reference evapotranspiration (mm dia<sup>-1</sup>),  $R_n$  is the net radiation (MJ m<sup>-2</sup> day<sup>-1</sup>),  $G$  is the soil heat flux density (MJ m<sup>-2</sup> day<sup>-1</sup>),  $T$  is the mean daily air temperature at a height of 2 m (°C),  $U_2$  is the wind speed at a height of 2 m (m s<sup>-1</sup>),  $e_s$  is the saturated vapor pressure (kPa),  $e_a$  is the actual vapor pressure (kPa),  $\Delta$  is the slope vapor pressure curve (kPa °C<sup>-1</sup>), and  $\gamma$  is the psychrometric constant (kPa °C<sup>-1</sup>).

Due to the lack of  $U_2$  and  $R_s$  data, these two parameters were estimated (Eqs. (2) and (3)) based on the data for sunshine duration and  $U_{10}$ , respectively (Allen et al., 1998).

$$U_2 = U_{10} \frac{4.87}{\ln 67.8z - 5.42} \quad (2)$$

$$R_s = \left( a_s + b_s \frac{n}{N} \right) R_a \quad (3)$$

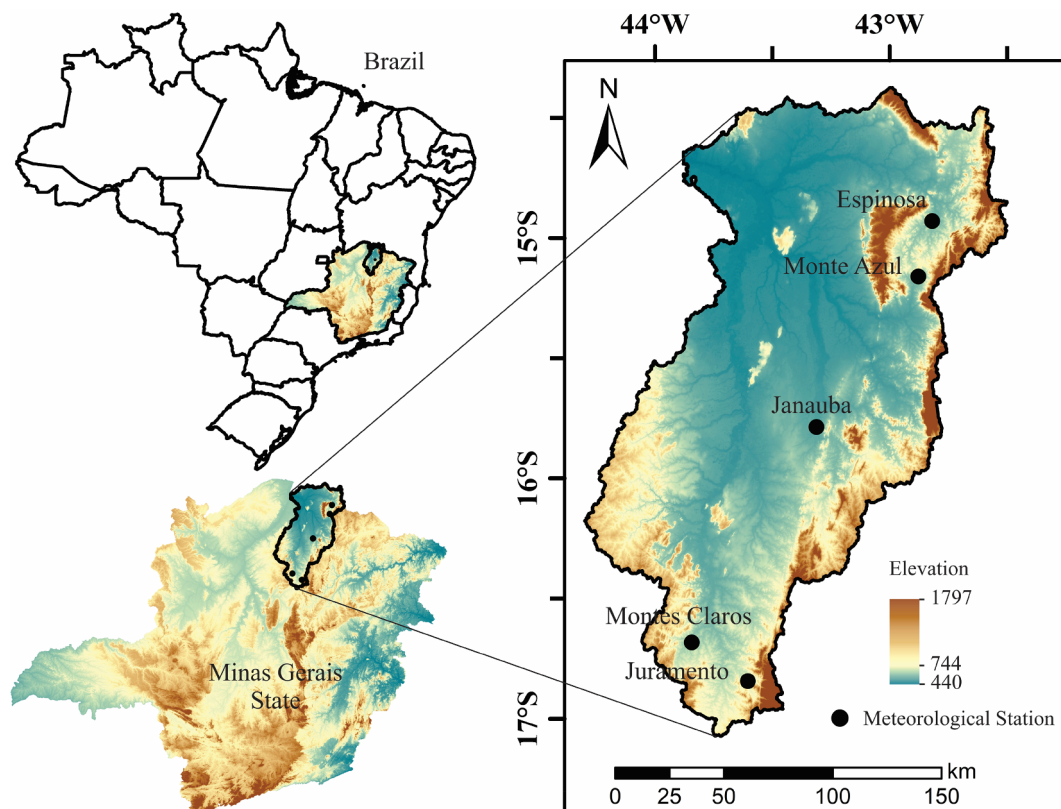


Fig. 1. Geographical location of the meteorological stations.

**Table 2**  
Multiple regression models tested to estimate  $ET_0$  ( $Z_i$ ) as a function of maximum ( $x_i$ ) and minimum ( $y_i$ ) temperatures.

Models	Function
1	$Z_i = a + bx_i + cy_i + e_i$
2	$Z_i = a + bx_i + cx_i^2 + dy_i + e_i$
3	$Z_i = a + bx_i + cy_i + dy_i^2 + e_i$
4	$Z_i = a + bx_i + cx_i^2 + dy_i + fy_i^2 + e_i$
5	$Z_i = a + bx_i + cy_i + dx_iy_i + e_i$
6	$Z_i = a + bx_i + cx_i^2 + dy_i + fx_iy_i + e_i$
7	$Z_i = a + bx_i + cy_i + dy_i^2 + fx_iy_i + e_i$
8	$Z_i = a + bx_i + cx_i^2 + dy_i + fy_i^2 + gx_iy_i + e_i$
9	$Z_i = a + bx_i + cx_i^2 + dy_i + fy_i^2 + gx_iy_i + hx_i^2y_i + e_i$
10	$Z_i = a + bx_i + cx_i^2 + dy_i + fy_i^2 + gx_iy_i + hx_iy_i^2 + e_i$
11	$Z_i = a + bx_i + cx_i^2 + dy_i + fy_i^2 + gx_iy_i + hx_i^2y_i + jx_iy_i^2 + e_i$
12	$Z_i = a + bx_i + cx_i^2 + dy_i + fy_i^2 + gx_iy_i + hx_i^2y_i + jx_iy_i^2 + k_i^2y_i^2 + e_i$

where  $U_{10}$  is the wind speed at a height of 10 m ( $m s^{-1}$ ),  $z$  is the height measurement (10 m),  $R_s$  is the solar or shortwave radiation ( $MJ m^{-2} day^{-1}$ ),  $n$  is the sunshine duration (h),  $N$  is the maximum possible sunshine or daylight duration (h),  $R_a$  is extraterrestrial radiation ( $MJ m^{-2} dia^{-1}$ ), and  $a_s$  and  $b_s$  are constants with a value of 0.28 and 0.52, respectively, as recommended by FAO-56 (Allen et al., 1998).

2.3. Hargreaves Samani model

The Hargreaves Samani (HS) model (Eq. (4)) was initially proposed by Hargreaves and Samani (1985) and requires only air temperature data to estimate  $ET_0$ .

$$ET_0 = 0.0023R_a (T_{max} - T_{min})^{0.5}(T + 17.8) \tag{4}$$

where  $T_{max}$  and  $T_{min}$  are the maximum and minimum air temperatures ( $^{\circ}C$ ), respectively.

The extraterrestrial radiation data ( $R_a$ ) were calculated based on latitude data (Equation (5)).

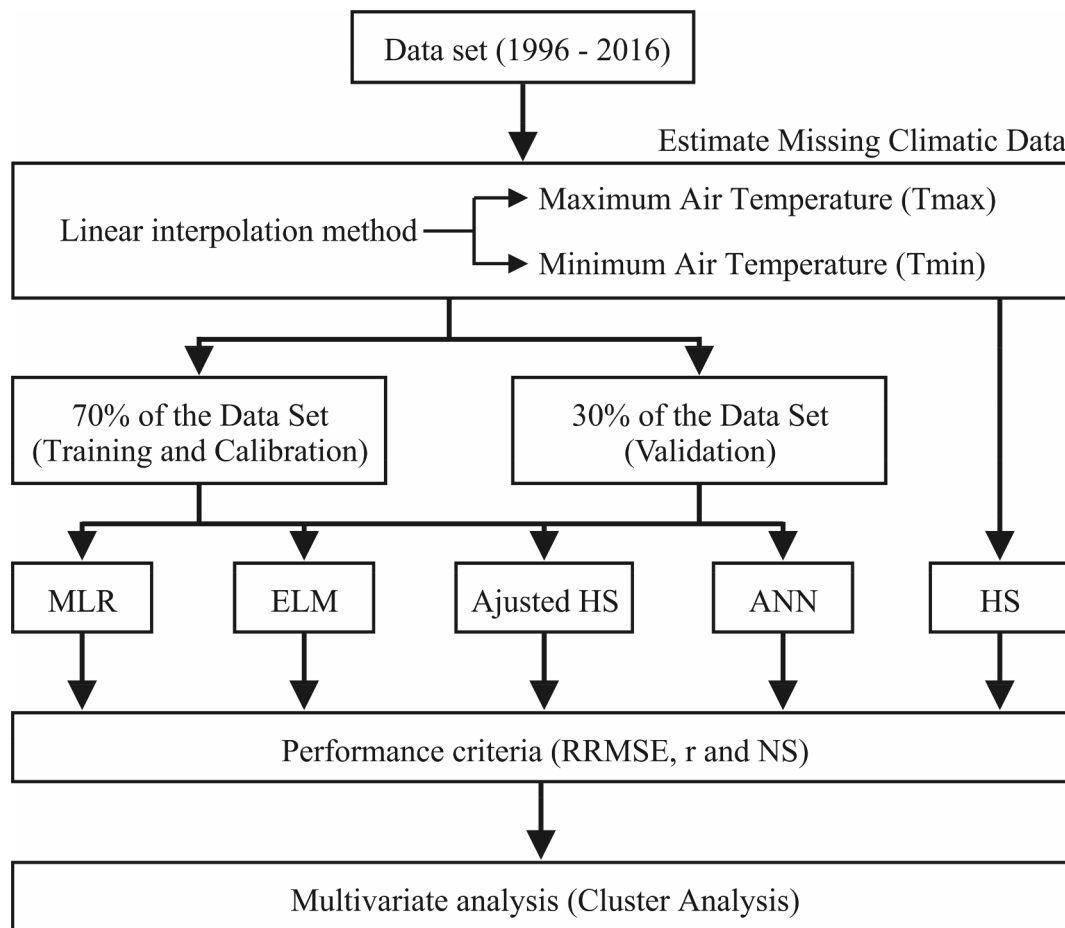
$$R_a = \frac{24(60)}{\pi} G_{SC} d_r [\omega_s \sin(\varphi) \sin(\delta) + \cos(\varphi) \cos(\delta) \cos(\omega_s)] \tag{5}$$

where  $R_a$  is the extraterrestrial radiation ( $MJ m^{-2} d^{-1}$ ),  $G_{SC}$  is the solar constant ( $0.0820 MJ m^{-2} min^{-1}$ ),  $d_r$  is the inverse relative Earth-Sun distance,  $\omega_s$  is the sunset hour angle (rad),  $\varphi$  is the latitude (rad) and  $\delta$  is the solar declination (rad).

The adjusted HS model was obtained by regression (Eq. (6)), which is an accepted and commonly used practice (Droogers and Allen, 2002; Feng et al., 2017b; Shiri et al., 2014).

$$ET_0^{PM} = a + bET_0^{HS} \tag{6}$$

where  $ET_0^{PM}$  is  $ET_0$  estimated by FAO-56 PM,  $ET_0^{HS}$  is  $ET_0$  estimated by



\*The Penman-Monteith equation was used to estimate  $ET_0$  data used as the targets for calibration and evaluation of adjusted HS, MLR, ANN and, ELM models.

**Fig. 2.** Workflow of the  $ET_0$  estimation in this study. MLR – multiple linear regression; ELM – extreme learning machine; HS – Hargreaves Samani; ANN – artificial neural Network “multilayer perceptron”; RRMSE - relative root mean square error; r - Pearson correlation coefficient; NS – Nash-Sutcliffe coefficient.

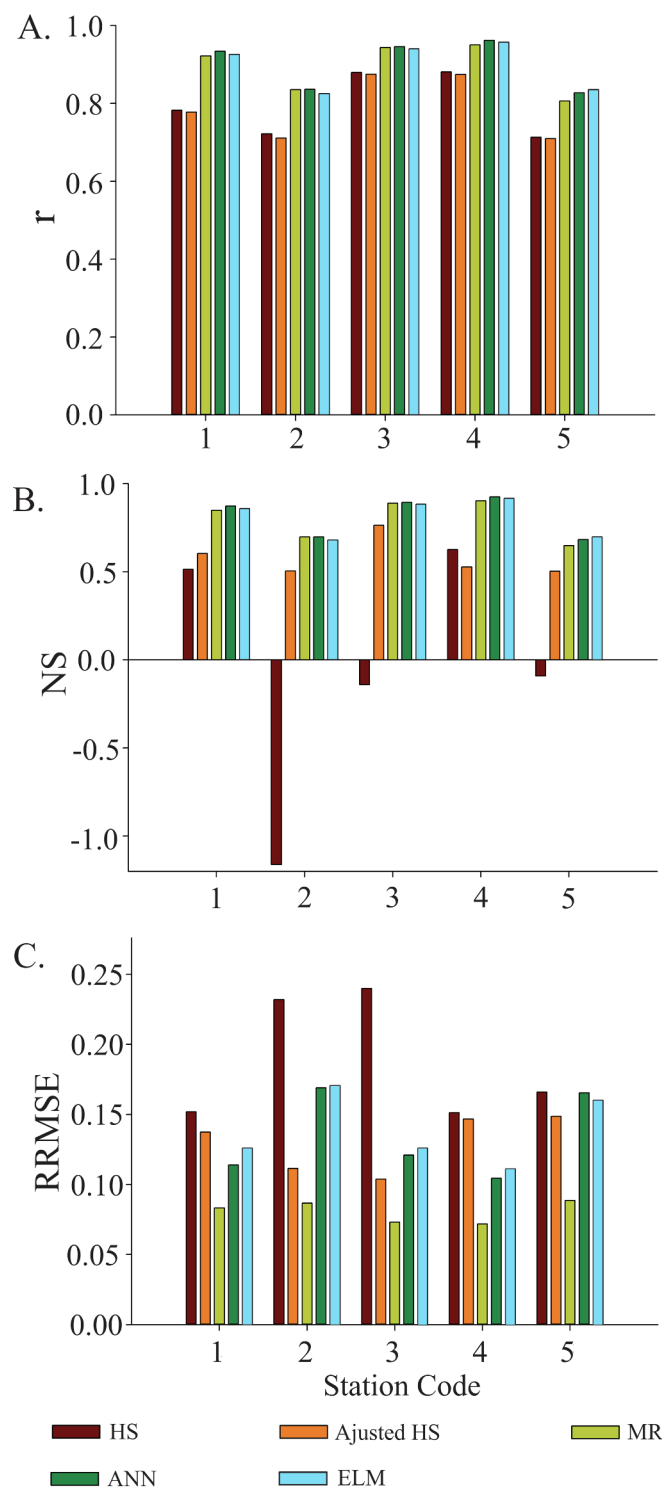


Fig. 3. Pearson correlation coefficient (r) (A), Nash-Sutcliffe coefficient (NS) (B) and relative root mean square error (RRMSE) (C) of the models during the study period (1996 to 2016) in the local scenario.

HS, and a and b are regression coefficients.

#### 2.4. Artificial neural networks

Artificial Neural Networks (ANNs) are mathematical models that are analogous to biological neural networks, which have been applied in many studies to model  $ET_0$  (Dou and Yang, 2018; Traore et al., 2010).

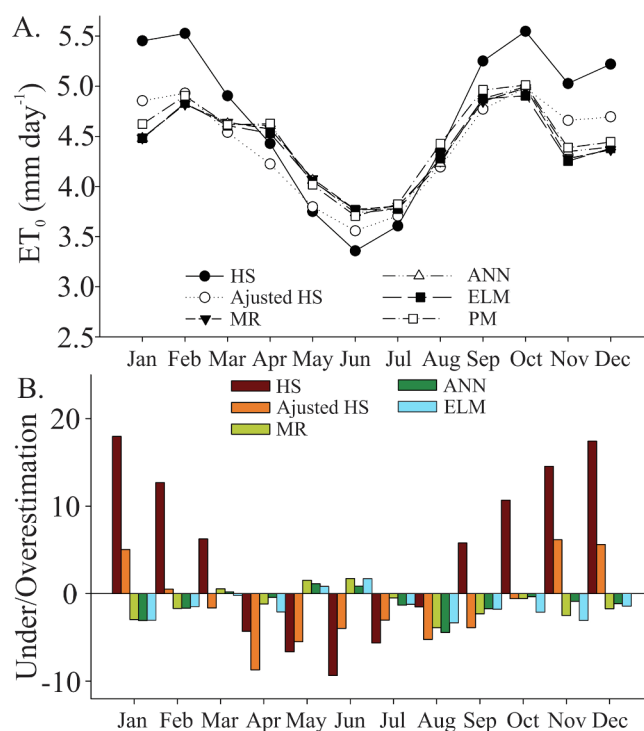


Fig. 4. Monthly variation in  $ET_0$  values estimated by PM, HS, adjusted HS, MLR, ANN and ELM models generated with local data (A) and under/overestimation values of HS, adjusted HS, MLR, ANN and ELM models in relation to the PM model (B).

Multilayer “perceptron” (MLP) networks have been used with “backpropagation” learning. For the development of MLP networks, the *mlp* function of the RSNNS package in the R software was used, with the *backpropagation* algorithm (*learnFunc* = “*Std\_Backpropagation*”) and a learning rate of 0.1 (*learnFuncParams* = 0.1). The networks were composed of an input layer with two neurons, corresponding to the number of input variables (Tmax and Tmin). In the output layer, a neuron corresponding to  $ET_0$  was introduced. To define the number of neurons in the hidden layer, a trial and error procedure was used. For this procedure, 1000 networks were tested with a number of neurons in the middle layer ranging from 1 to 10. The most appropriate model for the studied five cities was the one that presented eight neurons in the hidden layer, presenting smaller estimates of the mean square error.

The common sigmoid and linear activation functions were used for the hidden and output layers, respectively. The number of training times was arbitrated as 500.

#### 2.5. Multiple linear regression

To estimate  $ET_0$  from the maximum and minimum temperature, regression was also used. For this procedure, 12 regression models were tested (Table 2), and the quality of the fit was evaluated by estimating the Akaike information criterion (AIC). To adjust the regression models, we used the *lm* function in software R.

#### 2.6. Extreme learning machine

The ELM learning machine technique was initially proposed by Huang et al. (2006), and it has been applied in several studies on  $ET_0$  estimation (Dou and Yang, 2018; Feng et al., 2017b; Gocic et al., 2016) and in other research areas (Cao et al., 2016; Duan et al., 2016). ELM has an extremely fast learning speed in comparison to other learning machine techniques such as ANN. In addition, the number of neurons in the hidden layer for a specific ELM model does not need to be obtained



**Table 3**

Algebraic equations generated by multiple linear regression (MLR) and Hargreaves Samani (HS) models adjusted to estimate ET<sub>0</sub> in the local scenario.

City	Algebraic equation		R <sup>2</sup>	Adjusted HS	R <sup>2</sup>
	MLR				
Espinosa	$ET_0 = -42.3^{ns} + 2.564^{ns}(Tmax) - 0.04672^{ns}(Tmax^2) + 5.242(Tmin) - 0.2121^{**}$ $(Tmin^2) - 0.259^{ns}(Tmax)(Tmin) + 0.004269^{ns}(Tmax^2)(Tmin) + 0.01022^*(Tmax)(Tmin^2)$ $- 0.0001443^*(Tmax^2)(Tmin^2)$		0.85	$ET_0 = 1.22735^{***} + 0.78699^{***}ET_0^{HS}$	0.59
Janauba	$ET_0 = 23.761^{***} - 1.4303^{***}(Tmax) + 0.022346^{***}(Tmax^2) - 1.3629^{***}(Tmin) - 0.005278^{***}$ $(Tmin^2) + 0.09384^{***}(Tmax)(Tmin) - 0.0013245^{***}(Tmax^2)(Tmin)$		0.70	$ET_0 = 2.25225^{***} + 0.42465^{***}ET_0^{HS}$	0.50
Juramento	$ET_0 = 10.329^{***} - 0.43629^{**}(Tmax) + 0.004605^{ns}(Tmax^2) - 1.326^{***}(Tmin) + 0.0159^{**}$ $(Tmin^2) + 0.06947^{***}(Tmax)(Tmin) - 0.000544^{***}(Tmax^2)(Tmin) - 0.000754^{***}(Tmax)(Tmin^2)$		0.89	$ET_0 = 0.63383^{***} + 0.69692^{***}ET_0^{HS}$	0.76
Montes Claros	$ET_0 = 4.059^* + 0.1218^{ns}(Tmax) - 0.0111^{***}(Tmax^2) - 1.332^{***}(Tmin) + 0.02688^*$ $(Tmin^2) + 0.0694^{***}(Tmax)(Tmin) - 0.001942^{***}(Tmax)(Tmin^2) + 0.0000113^{ns}(Tmax^2)(Tmin^2)$		0.90	$ET_0 = 0.18561^{***} + 0.87316^{***}ET_0^{HS}$	0.76
Monte Azul	$ET_0 = 94.72^{**} - 5.948^{**}(Tmax) + 0.09489^{**}(Tmax^2) - 8.301^*(Tmin) + 0.1764^*(Tmin^2) + 0.5284^*$ $(Tmax)(Tmin) - 0.008155^*(Tmax^2)(Tmin) - 0.01113^*(Tmax)(Tmin^2) + 0.0001712^*(Tmax^2)(Tmin^2)$		0.68	$ET_0 = 2.48186^{***} + 0.50762^{***}ET_0^{HS}$	0.51

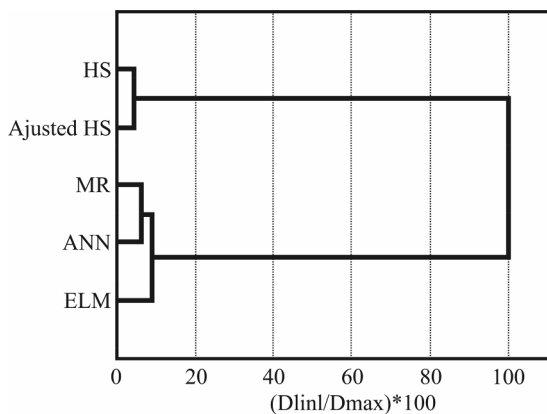
Tmax – maximum temperature; Tmin – minimum temperature; R<sup>2</sup> – coefficient of determination; ns – not significant by Student’s t test; and \*, \*\*, \*\*\* significant at levels of 0.05, 0.01 and 0.001 by Student’s t test, respectively.

**Table 4**

Global average performance and annual average of ET<sub>0</sub> values estimated by the HS, adjusted HS, MLR, ANN and ELM models generated with local data.

Model	r	NS	RRMSE	ET <sub>0</sub> (mm)	Under/Overestimation (%)
HS	0.663	-0.042	0.157	1714.7	4.8
Adjusted HS	0.658	0.484	0.101	1608.3	-1.3
MLR	0.743	0.665	0.068	1608.1	-1.1
ANN	0.751	0.678	0.112	1609.5	-1.1
ELM	0.747	0.672	0.116	1603.0	-1.4
PM	/	/	/	1627.5	/

r – Pearson correlation coefficient; NS – Nash-Sutcliffe coefficient; RRMSE – relative root mean square error; ET<sub>0</sub> – reference evapotranspiration; HS – Hargreaves Samani; MLR – multiple linear regression; ANN – artificial neural networks; ELM – extreme learning machine; PM – Penman-Monteith.



**Fig. 5.** Hierarchical dendrogram obtained by the Ward algorithm for the HS, adjusted HS, MLR, ANN and ELM models generated with local data.

by a trial and error procedure, as in the case of models generated by ANNs. In addition, adjustment of all the parameters (e.g., the input weights and biases) in relation to the hidden neurons is not required because these parameters are independent of the training data. More details about the ELM model can be found in Huang et al. (2006) and Gocic et al. (2016).

The ELM model consists of an input layer with two neurons (Tmax and Tmin), a single hidden layer with six neurons and the output layer (ET<sub>0</sub>). For the generation of ELM models, the *elmtrain* function of the *elmNN* package in R software was used. The symmetric saturating linear transfer function and the linear function were used in the hidden and output layers, respectively.

**2.7. Calibration and validation of the models**

In this study, 70% of the data set was used for training and calibration, while the remaining 30% was used for validation of the adjusted HS, MLR, ANN and ELM models. This division was performed through the *splitForTrainingAndTest* function of the RSNNS package in R software. To ensure that the data set was randomly distributed between the training set and the validation set, the data were previously randomized using the *sample* function of the *base* package in R software.

All the input data from the ELM and ANN models were normalized (ranging from 0 to 1) to minimize the influence of the absolute scale. The normalization scheme is defined by Eq. (7).

$$x_{norm} = \frac{x_0 - x_{min}}{x_{max} - x_{min}} \tag{7}$$

where  $x_{norm}$ ,  $x_0$ ,  $x_{min}$  and  $x_{max}$  are the normalized value, real value, minimum value and maximum value, respectively.

For normalization, the *normalizeData* function of the RSNNS package in R software was used.

The normalized data for ET<sub>0</sub> obtained by the ANN and ELM models were transformed into mm day<sup>-1</sup> unit using Eq. (8).

$$V_{dn} = [V_{max} + (V_n - 1)(V_{max} - V_{min})] \tag{8}$$

where  $V_{dn}$  is the denormalized value (dimensionless),  $V_n$  is the normalized value,  $V_{min}$  is the minimum value of the sample, and  $V_{max}$  is the maximum value of the sample.

The ANN and ELM models were tested 1000 times, storing their respective mean squared errors (MSE) for the validation data set. The MSE for the validation sample was determined using Eq. (9).

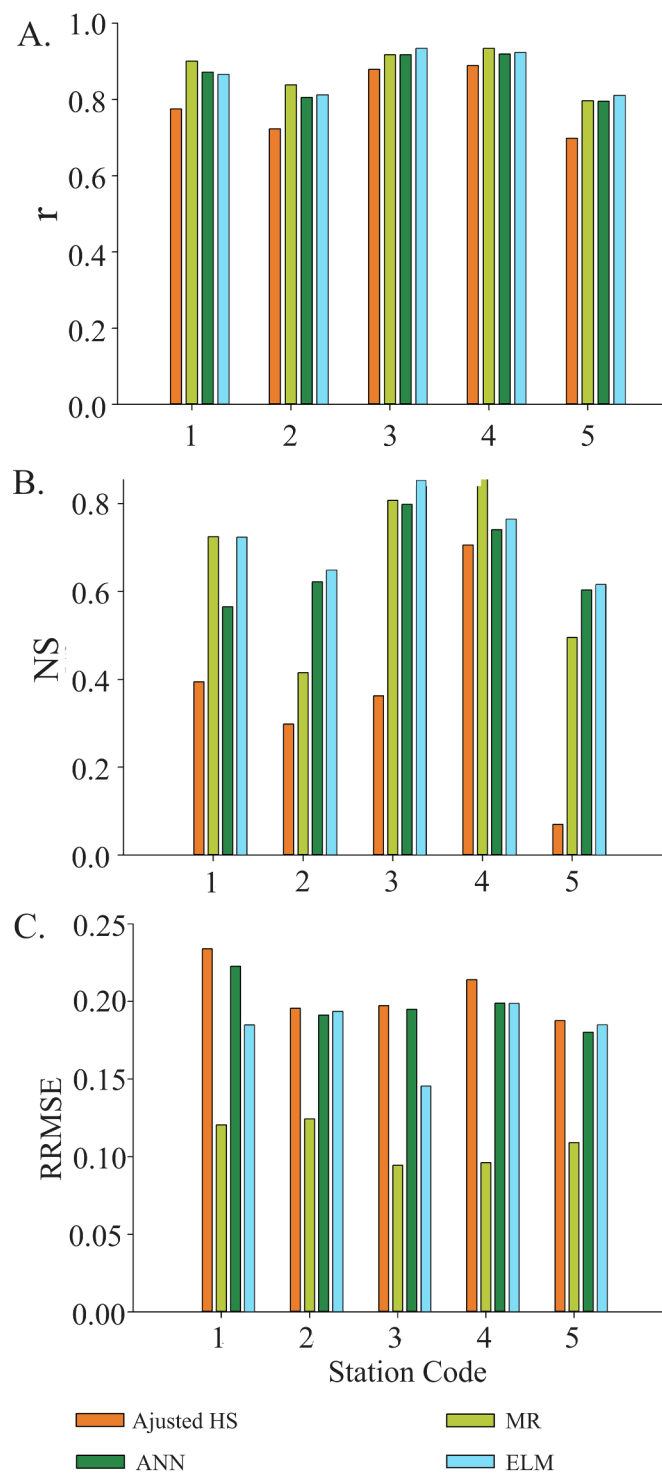
$$MSE = \frac{\sum_{i=1}^n (P_i - O_i)^2}{n} \tag{9}$$

where n is the total number of data tested, and  $P_i$  and  $O_i$  are the ET<sub>0</sub> values obtained by the FAO-56 PM method and by the artificial intelligence methods (ANN and ELM), respectively.

The best fit network for the ANN and ELM models was established by the smaller MSE for the validation sample, with the objective to ensure the absence of overfitting.

**2.8. Performance criteria**

The relative root mean square error (RRMSE) (Eq. (10)), Pearson correlation coefficient (r) (Eq. (11)) and Nash-Sutcliffe coefficient (NS) (Eq. (12)) were used to evaluate the performance of the HS, adjusted HS, MLR, ANN and ELM models.



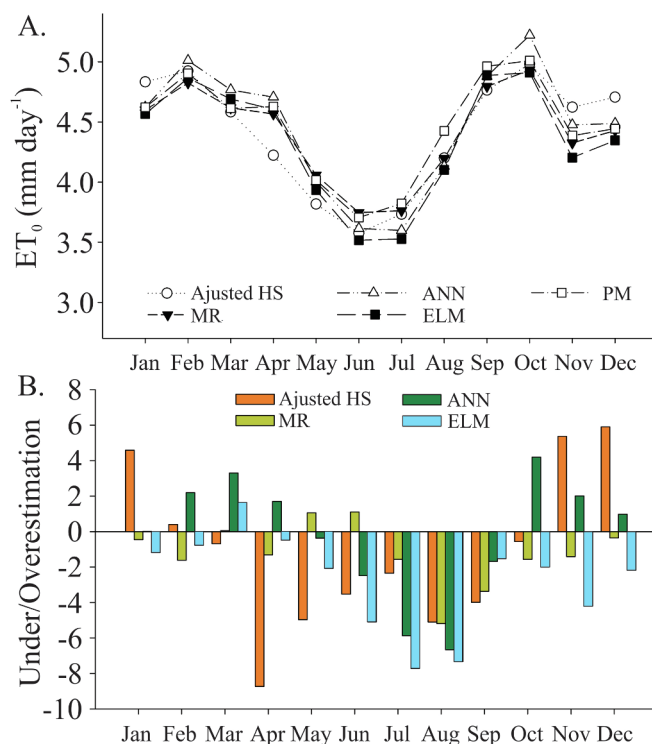
**Fig. 6.** Pearson correlation coefficient (r) (A), Nash-Sutcliffe (NS) coefficient (B) and relative root mean square error (RRMSE) (C) of the adjusted HS, MLR, ANN and ELM models generated with pooled data.

**Table 5**

Algebraic equations generated by multiple linear regression (MLR) and Hargreaves Samani (HS) models, adjusted to estimate ET<sub>0</sub> in the pooled scenario.

Scenario	Algebraic equation	R <sup>2</sup>	Adjusted HS	R <sup>2</sup>
Pooled	MLR ET <sub>0</sub> = - 3.12 <sup>**</sup> + 0.03771 <sup>ns</sup> Tmax + 0.00263 <sup>ns</sup> Tmax <sup>2</sup> + 0.958 <sup>***</sup> Tmin - 0.07869 <sup>***</sup> Tmin <sup>2</sup> - 0.01941 <sup>***</sup> Tmax Tmin + 0.003502 <sup>***</sup> Tmax (Tmin <sup>2</sup> ) - 0.00003909 <sup>***</sup> (Tmax <sup>2</sup> ) (Tmin <sup>2</sup> )	0.75	ET <sub>0</sub> = 1.45886 <sup>***</sup> + 0.63267 <sup>***</sup> ET <sub>0</sub> <sup>HS</sup>	0.49

Tmax – maximum temperature; Tmin – minimum temperature; R<sup>2</sup> – coefficient of determination; ns – not significant by Student’s *t* test; and \*, \*\*, \*\*\* Significant at levels of 0.05, 0.01 and 0.001 by Student’s *t* test, respectively.



**Fig. 7.** Monthly variation of ET<sub>0</sub> values estimated by PM, HS, adjusted HS, MLR, ANN and ELM models generated with pooled data (A), and under/overestimation values of HS, adjusted HS, MLR, ANN and ELM models in relation to the PM model (B).

**Table 6**

Global average performance and annual average of ET<sub>0</sub> values estimated by adjusted HS, MLR, ANN and ELM models generated with pooled data.

Model	r	NS	RRMSE	ET <sub>0</sub> (mm)	Under/Overestimation (%)
Adjusted HS	0.661	0.305	0.171	1610.1	-1.1
MLR	0.731	0.550	0.091	1606.7	-1.2
ANN	0.718	0.555	0.165	1626.4	-0.2
ELM	0.724	0.601	0.151	1585.1	-2.7
PM	/	/	/	1627.5	/

r – Pearson correlation coefficient; NS – Nash-Sutcliffe coefficient; RRMSE – relative root mean square error; ET<sub>0</sub> – reference evapotranspiration; HS – Hargreaves Samani; MLR – multiple linear regression; ANN – artificial neural networks; ELM – extreme learning machine; PM – Penman-Monteith.

$$RRMSE = \frac{RMSE}{P_i} = \frac{\sqrt{\frac{1}{n} \sum_{i=1}^n (P_i - O_i)^2}}{\bar{P}_i} \tag{10}$$

$$r = \frac{n(\sum_{i=1}^n O_i \cdot P_i) - (\sum_{i=1}^n O_i) \cdot (\sum_{i=1}^n P_i)}{\sqrt{(n \sum_{i=1}^n O_i^2 - (\sum_{i=1}^n O_i)^2) \cdot (n \sum_{i=1}^n P_i^2 - (\sum_{i=1}^n P_i)^2)}} \tag{11}$$

$$NS = 1 - \frac{\sum_{i=1}^n (O_i - P_i)^2}{\sum_{i=1}^n (P_i - \bar{P}_i)^2} \tag{12}$$

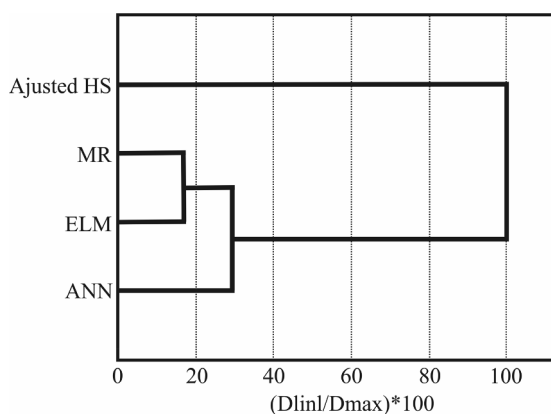


Fig. 8. Hierarchical dendrogram obtained by the Ward algorithm for the MLR, adjusted HS, ANN and ELM models generated with pooled data.

where  $n$  is the total number of data tested, and  $P_i$  and  $O_i$  are the  $ET_0$  values obtained by the FAO-56 PM method and by the other methods (HS, adjusted HS, MLR, ANN and ELM), respectively. RRMSE is dimensionless and presents the perfect fit with a result of 0. The NS and  $r$  coefficients are dimensionless and have the perfect fit with a result of 1.

## 2.9. Multivariate analysis

A multivariate analysis of the data set was performed using cluster analysis (CA). The  $ET_0$  data for the HS, adjusted HS, MLR, ANN, and ELM models were previously standardized to avoid misclassification due to size differences of the data. Subsequently, standardized Euclidean distances as similarity measure were estimated. CA was performed in the data set by the Ward method (Ward, 1963).

## 2.10. Data processing

Fig. 2 shows the workflow of the  $ET_0$  estimation in this study.

## 3. Results and discussion

### 3.1. Local implementation of the models

The MLR, ANN and ELM models, based on air temperature data, presented similar performance criteria (RRMSE,  $r$  and NS), with  $r$  varying between 0.962 and 0.806 (Fig. 3A), NS ranging from 0.926 to 0.648 (Fig. 3B), and RRMSE ranging from 0.171 to 0.072 (Fig. 3C). The MLR model showed the lowest RRMSE in all cities. In the cities of Espinosa (station 1), Janaúba (station 2), Juramento (station 3) and Montes Claros (station 4), the ANN model had the highest  $r$  and NS values, while in the city of Monte Azul (station 5), the  $r$  and NS indexes were higher in the ELM model. The MLR, ANN and ELM models, adjusted for the city of Montes Claros (station 4), presented the best performance criteria (RRMSE,  $r$  and NS) compared to the other cities (Fig. 3). The algebraic equations that best estimated  $ET_0$  for the MLR and adjusted HS models in the local scenario are presented in Table 3.

The ANN, ELM and MLR models were more accurate than the original and adjusted HS empirical models, according to RRMSE,  $r$  and NS performance criteria. The original HS model had higher accuracy in the city of Montes Claros (station 4), with  $r$ , NS and RRMSE of 0.881, 0.626 and 0.151, respectively. In contrast, the adjusted HS model showed higher precision in the city of Juramento (station 3), with  $r$ , NS and RRMSE of 0.875, 0.763 and 0.104, respectively. Regarding the original HS model, the cities of Janaúba (station 2), Juramento (station 3) and Monte Azul (station 5) presented the least accurate results, with NS of  $-1.162$ , RRMSE of 0.240 and  $r$  of 0.713, respectively, while the adjusted HS model had lower accuracy in Monte Azul (station 5), with  $r$ ,

NS and RRMSE of 0.710, 0.503 and 0.149, respectively. The use of regression made the  $ET_0$  estimate more accurate by the adjusted HS model compared to the original HS equation (Fig. 3).

Considering the PM model (FAO 56 – PM) as a reference, the original HS model overestimated  $ET_0$  in January, February, March, September, October, November and December and underestimated it in the other months. Regarding the adjusted HS, the model overestimated  $ET_0$  in January, February, November and December and underestimated it in the other months. The behavior presented by the original and adjusted HS models is consistent with the studies reported by Allen et al. (1998), Didari and Ahmadi (2019), and Droogers and Allen (2002), where the HS model also tended to overestimate  $ET_0$  under conditions of high relative humidity. The  $ET_0$  values of the MLR, ANN and ELM models were closer to the  $ET_0$  values estimated by the PM model compared to the adjusted HS and HS models. The MLR, ANN and ELM models showed underestimated and overestimated values ranging from  $-3.89$  to 1.71%,  $-4.44$  and 1.12%, and  $-3.32$  and 1.70%, respectively (Fig. 3).

Table 4 shows the global average performance of the models generated with local data, considering the joint evaluation of the five stations analyzed during the study period. The HS model overestimated  $ET_0$  by 4.8%, while the adjusted HS, MLR, ANN and ELM models underestimated 1.3, 1.1, 1.1 and 1.4%, respectively (Table 4). The ANN models (with  $r$  of 0.751 and NS of 0.687) and MLR (with RRMSE of 0.068) presented higher global precision, in addition to providing annual mean  $ET_0$  values closer to those of the reference model, FAO 56 – PM (Table 4). The original HS was the model with the lowest global accuracy, with NS of  $-0.042$  and RRMSE of 0.157; in addition, the annual mean  $ET_0$  estimated by the original HS differed by 87.2 mm from the reference model (FAO 56 – PM), while showing differences between 2.5 and 18.0 mm with respect to the other models (Table 4).

The HS, adjusted HS, MLR, ANN and ELM models were grouped into two clusters (Fig. 5). Cluster 1 consisted of HS and adjusted HS, models that presented the worst performance coefficients (Fig. 3 and Table 4), and  $ET_0$  values farther from the reference model, FAO-56 PM (Fig. 4 and Table 4). Cluster 2 was formed by the MLR, ANN and ELM models (Fig. 5).

The MLR, ANN and ELM models presented the best performance coefficients (Fig. 3 and Table 4) and mean monthly and annual  $ET_0$  values closer to the reference model, FAO-56 PM (Fig. 4 and Table 4), in addition to being grouped in the same Cluster (Fig. 5). In the local scenario, these results indicate the applicability of ANN and ELM artificial intelligence methods and the MLR model to estimate  $ET_0$  using only temperature data.

### 3.2. Pooled implementation of the models

Similar to the local scenario, the MLR, ANN and ELM models generated with the pooled temperature data from the five stations showed similar performance, with  $r$  varying between 0.934 and 0.795 (Fig. 6A), NS ranging from 0.858 to 0.415 (Fig. 6B), and RRMSE ranging from 0.223 to 0.094 (Fig. 6C). The MLR model had better performance in the cities of Espinosa (station 1, with  $r$  of 0.900, NS of 0.725 and RRMSE of 0.120), Janaúba (station 2, with  $r$  of 0.838 and RRMSE of 0.124) and Montes Claros (station 4, with  $r$  of 0.934, NS of 0.858 and RRMSE of 0.096), while the ELM model performed better in the cities of Juramento (station 3, with  $r$  of 0.934 and NS of 0.853) and Monte Azul (station 5, with  $r$  of 0.811 and NS of 0.616) (Fig. 6). The adjusted HS model had the worst performance in all cities, with  $r$  ranging from 0.899 to 0.698 (Fig. 6A), NS ranging from 0.706 to 0.070 (Fig. 6B), and RRMSE ranging from 0.234 to 0.188 (Fig. 6C). The algebraic equations that best estimated  $ET_0$  for the MLR and adjusted HS models, in the pooled data scenario, are presented in Table 5.

Similar to the local scenario, MLR and ELM models underestimated  $ET_0$  during most of the year, showing monthly mean values that were higher than the PM model (FAO 56 – PM) only in March, May and June,



when the MLR model was analyzed, and March, when the ELM model was analyzed. The ANN model underestimated  $ET_0$  during the dry and cold period of the year (May to September), while the adjusted HS model overestimated  $ET_0$  in January, February, November, and December. The adjusted HS, MLR, ANN and ELM models presented underestimated and overestimated values ranging from  $-8.74$  to  $5.91\%$ ,  $-5.19$  and  $1.11\%$ ,  $-6.65$  and  $4.20\%$ , and  $-7.73$  and  $1.64\%$ , respectively (Fig. 7).

Table 6 shows the global average performance of the models generated with pooled data, considering the joint evaluation of the five stations analyzed during the study period. The adjusted HS, MLR, ANN and ELM models underestimated  $ET_0$  by 1.1, 1.2, 0.2, and 2.7%, respectively (Table 6). The MLR (with  $r$  of 0.731 and RRMSE of 0.091) and ELM (with NS of 0.601) models presented the best global performance, although the ANN model provided annual mean  $ET_0$  values closer to the reference model (FAO 56 – PM) (Table 6). The adjusted HS model had the worst global performance, with  $r$  of 0.661, NS of 0.305 and RRMSE of 0.171 (Table 6).

The MLR, adjusted HS, ANN and ELM models were grouped into two clusters (Fig. 8). Cluster 1 was formed by the adjusted HS, the model that presented the worst performance coefficients (Fig. 6 and Table 6). Cluster 2 was formed by the MLR, ANN and ELM models (Fig. 8).

Similar to the observations in the local scenario, the MLR, ANN and ELM models had the best performance coefficients (Fig. 6 and Table 6) and were grouped in the same cluster (Fig. 8) in the pooled data scenario. These results indicated the best applicability of ANN and ELM artificial intelligence methods and the MLR model to estimate  $ET_0$ , using only temperature data.

The artificial intelligence methods (e.g., ANN and ELM) usually perform better than linear models (e.g., MLR) because they are efficient for modeling phenomena of linear and nonlinear nature, as well as considering possible interactions between variables. The MLR model used in this research presented similar results to the models based on artificial intelligence (ANN and ELM), as observed in other studies (Huo et al., 2012; Ribeiro et al., 2019; Tabari et al., 2012). This can be justified by the fact that the linear, quadratic and interaction effects were considered in some of the MLR models.

The locally trained models were more accurate than the models with pooled temperature data, which is consistent with the data reported by Shiri et al. (2014) in Iran and contrasts with the work of Feng et al. (2017b) in China. However, the generation of models using a combined approach allows the estimation of  $ET_0$  in cases of unavailability of local meteorological data.

The present study confirmed the ability of the ANN, ELM and MLR models to estimate  $ET_0$  only with air temperature data as input. Compared with the ANN model based on MLP, the ELM demonstrated much faster performance when executing the training and testing processes in R software. The MLR models were easier to apply because they provide explicit algebraic equations for the calculation of  $ET_0$  (Table 3 and 5).

Therefore, ANN, ELM and MLR models can be used in irrigation planning and management, thus allowing more precise estimation of crop water requirements through air temperature data; however, the MLR model presents the advantage of the use of explicit algebraic equations, which facilitates their use by farmers and technicians to accurately estimate  $ET_0$ .

#### 4. Conclusions

In this study, the applicability of the Hargreaves Samani (HS), adjusted HS, artificial neural network (ANN), multiple linear regression (MLR) and extreme learning machine (ELM) models was evaluated to estimate the reference evapotranspiration ( $ET_0$ ) based on temperature data from the Verde Grande River basin, southeastern Brazil. This study was carried out in two parts. In the first part (local scenario), all the

models were trained, calibrated and validated separately at each station. In the second part (pooled scenario), the meteorological data from all the stations were grouped to train and calibrate the models and then tested separately at each station. To test and validate the models, the Penman-Monteith model (FAO-56 PM) for  $ET_0$  estimation was considered as a reference. The main conclusions can be summarized as follows.

- (1) The ANN, MLR and ELM models showed a great ability to estimate  $ET_0$ ; moreover, they were more accurate than the original and adjusted HS models, both in the local and pooled scenarios.
- (2) The ANN, MLR and ELM models had very similar accuracies, but the MLR models were easier to use, as they calculated the  $ET_0$  using explicit algebraic equations.
- (3) Although the ANN, MLR and ELM models showed better adjustment in the local scenario, in the pooled scenario, these models allowed the accurate estimation of  $ET_0$  in cases of unavailability of local meteorological data.
- (4) The use of the linear regression model to fit the HS equation increased the accuracy of this model to estimate  $ET_0$ .

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