

Angle-tunable intersubband photoabsorption and enhanced photobleaching in twisted bilayer graphene

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ABSTRACT

Van der Waals heterostructures obtained by artificially stacking two-dimensional crystals represent the frontier of material engineering, demonstrating properties superior to those of the starting materials. Fine control of the interlayer twist angle has opened new possibilities for tailoring the optoelectronic properties of these heterostructures. Twisted bilayer graphene with a strong interlayer coupling is a prototype of twisted heterostructure inheriting the intriguing electronic properties of graphene. Understanding the effects of the twist angle on its out-of-equilibrium optical properties is crucial for devising optoelectronic applications. With this aim, we here combine excitation-resolved hot photoluminescence with femtosecond transient absorption microscopy. The hot charge carrier distribution induced by photo-excitation results in peaked absorption bleaching and photo-induced absorption bands, both with pronounced twist angle dependence. Theoretical simulations of the electronic band structure and of the joint density of states enable to assign these bands to the blocking of interband transitions at the van Hove singularities and to photo-activated intersubband transitions. The tens of picoseconds relaxation dynamics of the observed bands is attributed to the angle-dependence of electron and phonon heat capacities of twisted bilayer graphene.

KEYWORDS

twisted bilayer graphene, transient absorption microscopy, hot-photoluminescence, van der Waals heterostructures, optoelectronic properties, van Hove singularities

1 Introduction

Van der Waals heterostructures composed of stacked single-layer crystals represent a promising platform for novel electronic, photonic and spintronic devices [1–8]. Wide tunability of the optoelectronic properties is achieved by both selection of the stacked materials and control of the relative rotation between the crystal registries [5, 9, 10–12], i.e. the twist angle. In the case of two layers of graphene, strong interlayer coupling drives the hybridization of the electronic states and can lead to the formation of moiré super-lattices for finite twist angle. The rotational misalignment of twisted bilayer graphene (tBLG) enables to explore also new properties as topological valley transport [13], superconductivity [14] at the magic twist angle $\theta \sim 1.1^\circ$, or the topologically protected one-dimensional (1D) chiral states appearing at the moiré domain walls [15]. The Dirac cones associated to the two layers in tBLG are no longer aligned in the energy-momentum landscape and two saddle points appear at their low-energy intersections. The saddle points contribute to van Hove singularities (vHs) in the density

of states, which occur at energies E_{vHs} that depend on the twist angle [16]. The vHs are detected as a peak in the optical conductivity of tBLG [17–19] and they have been related to the increase of hot photoluminescence (PL) for resonant excitation [20]. These vHs appear at much lower energies than in single-layer graphene (SLG) [16, 21–24] and allow angle controlled visible and near-infrared (NIR) absorption enhancement. This property has been exploited in a tBLG based photo-detector to selectively increase the photocurrent generation at the vHs [25].

The changes in crystal symmetry, electronic band structure and optical conductivity come along with modifications of the relaxation pathways available to charge carriers driven out of equilibrium. The carrier dynamics in SLG is well-known as it has been intensively studied by means of ultrafast transient absorption (TA) [26–31], time-resolved photocurrent [32, 33] and photoemission spectroscopies [34–36]. Excitation with femtosecond light pulses produces out-of-equilibrium distributions of electrons and holes in the conduction and valence bands, which thermalize in ~ 50 fs via Coulomb

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two-body scattering to hot Fermi-Dirac (FD) distributions [30, 31]. The relaxation of the hot carriers proceeds through scattering with strongly coupled optical phonons (SCOP) till a common temperature is reached in about 200 fs. The cooling of the thermalized electron-phonon bath is finally driven by the lattice and achieved in less than 10 picoseconds via anharmonic decay of the hot phonons. In defected SLG, hot carriers can release their excess energy also by defect-mediated emission of acoustic phonons (supercollision mechanism), which occurs on a picosecond time scale dependent on substrate and defect densities [31, 33, 37–43]. The hot carrier distribution inhibits interband absorption over a broad energy range due to Pauli blocking, so that in the TA spectra of SLG a decreased absorption, or photo-bleaching (PB), signal is detected.

In Bernal stacked bilayer graphene, together with the PB band, Limmer et al. [44] observed a photoinduced absorption (PA) with a single decay time of 5 ps, about twice as long as the PB signal. The PA has been attributed to transitions between subbands formed within the conduction and the valence bands, named intersubband (ISB) transitions, which are absent in SLG since it lacks a subband structure. Also time- and angle-resolved photoemission spectroscopy (tARPES) has demonstrated long-living (up to 10 ps) population inversion in bilayer graphene [45, 46] attributed to the presence of a small gap. Previous studies in tBLG by TA microscopy [47, 48] and tARPES [49] have explored the twist-angle dependence and shown long decay times attributed to bound excitons and to states reached by two-photon absorption [48, 50].

Here we studied the out-of-equilibrium optical properties of tBLG as a function of the twist angle by femtosecond TA microscopy with high sensitivity, which allows to explore low excitation regimes in which the angle-dependent contribution from ISB transitions emerges. Specifically, we investigated heterostructures with the vHs located in the NIR and twist angle θ in the range of $\sim 6^\circ$ – 8° . The tBLG samples were prepared by chemical vapor deposition, as described in the Methods, and have tens of μm linear dimension. A lattice rotation in the real space by an angle θ corresponds to a rotation of θ in the phase-space of the hexagonal Brillouin zones (BZs), as

sketched in Figs. 1(a) and 1(b). Accordingly, the Dirac points of the two layers (see Fig. 1(c)), K_A and K_B , no longer coincide and are displaced by a momentum $\Delta K = 2K\sin(\theta/2)$, where $K = 4\pi/3a$ and $a \approx 0.246$ nm are the SLG lattice parameter [51]. The interlayer interactions perturb the Dirac cones of each layer causing the formation of minigaps with the same energy in the conduction and valence bands at the vHs, as is schematically shown in Fig. 1(c).

Figure 1(d) shows the optical microscope image of one of the investigated samples, named stack 1, measured in reflection. It consists of a large single-crystal SLG, with an inner brighter region, where a second graphene layer is stacked to form a bilayer single crystal. A first determination of the mutual orientation of the lattices in the bilayer domain is obtained by extrapolation of the hexagonal habits of the outer/inner growth regions, corresponding respectively to the 1st/2nd layer [52]. In stack 1, the hexagons are rotated by an angle $\theta = 7^\circ \pm 1^\circ$. The angle determination from the optical images is affected by a large uncertainty related to the definition of the single-crystals shape. Twist angle is usually measured by high-resolution transmission electron microscopy [53, 54], scanning tunneling microscopy [16] and lattice resolution atomic force microscopy [55]. Here we adopted an all-optical, far-field approach, based on measuring the hot-photoluminescence excitation (hot-PLE) spectrum under femtosecond laser excitation. As previously observed [20], due to the enhancement of pump absorption, a peak is expected in the bilayer emission when the laser is tuned at the vHs. In Fig. 1(e) the hot PL intensity of tBLG normalized to that of SLG ($I_{\text{tBLG}}/I_{\text{SLG}}$) is shown as function of laser excitation energy. The experimental data are fitted with a Gaussian function centered at $E_{\text{vHs}} = 1.388 \pm 0.007$ eV. From the energy of the vHs, we extracted a more accurate estimation of the twist angle considering the correlation θ ($^\circ$) = $A - \sqrt{(B - C \cdot E_{\text{vHs}})}$ (eV), with $A = 45.380$, $B = 2.030 \times 10^3$, $C = 4.186 \times 10^2$ extracted from the analysis of the calculated joint density of states (JDOS) as a function of θ reported in Fig. S1 in the Electronic Supplementary Material (ESM). We obtained the value $\theta = 7.31^\circ \pm 0.04^\circ$ for stack 1, in good agreement with the evaluation from the optical image inspection. The hot PL map in Fig. 1(e)

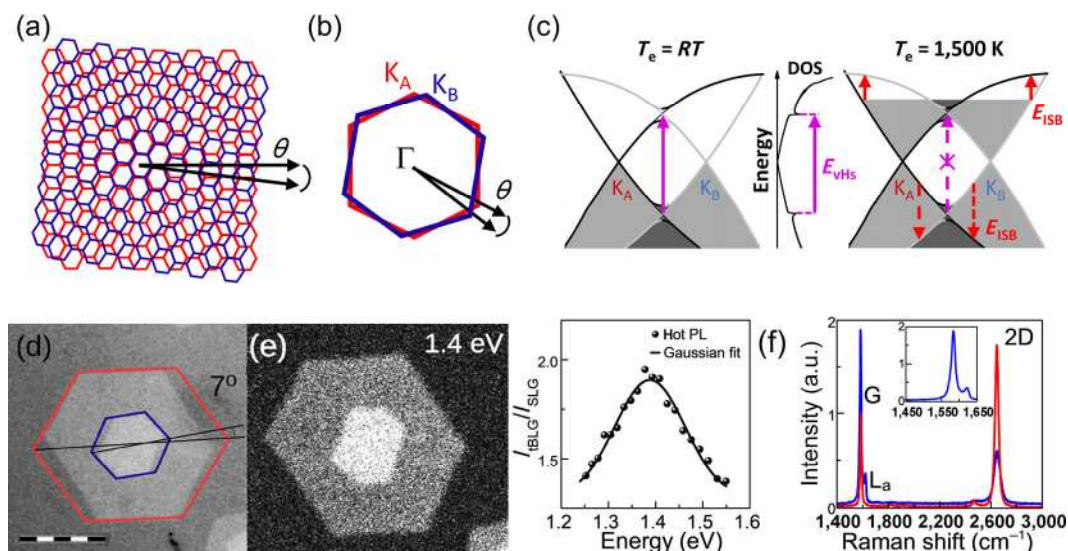


Figure 1 (a) Sketch of the crystal structure of a tBLG with twist angle θ ; (b) the corresponding BZs of two rotated graphene layers as the red and blue hexagons; (c) energy structure indicating the optical transition at the vHs at photon energy E_{vHs} (magenta line) and intersubband transitions from photo-excited FD distributions of electrons (red solid lines) and holes (red dashed lines); (d) bright field optical image of stack 1 with blue and red hexagons identifying a layer rotation angle of about 7° , scale bar $10 \mu\text{m}$; (e) PL intensity map for laser excitation energy of 1.4 eV, in resonance with the E_{vHs} identified by the peak in the PLE intensity of tBLG (I_{tBLG}) divided by that of the corresponding SLG (I_{SLG}); (f) Raman spectra of stack 1 at the bilayer (blue line) and monolayer (red line) regions normalized by the intensity of the G peak. The inset shows a zoom-in of the bilayer G and L_a peaks divided by the monolayer G peak.

for laser excitation tuned at 1.4 eV, close to E_{vHs} , reports indeed a ≈ 2 times higher emission intensity at the tBLG compared to the SLG, uniform across the bilayer domain.

Extra peaks have been observed in visible, IR and UV Raman spectra of tBLG compared to SLG. Accordingly, we characterized the heterostructure by micro-Raman spectroscopy using a visible laser tuned at 633 nm. Figure 1(f) shows the Raman spectra at the SLG (red line) and tBLG (blue line) regions. The G-band peak at $1,584\text{ cm}^{-1}$, the 2D peak at $2,648\text{ cm}^{-1}$ and an additional peak at $1,621\text{ cm}^{-1}$ are observed for tBLG, while for SLG these bands are observed at $1,588\text{ cm}^{-1}$ (G) and $2,645\text{ cm}^{-1}$ (2D).

In the bilayer, the G-band peak has a two times higher intensity, as shown in the inset of Fig. 1(f). The enhancements of the G-band and the extra peak, L_a , testify the formation of a new band structure by interlayer coupling. They are thus an indication of the high crystalline quality of the samples and of a clean interface between the two monolayers forming the tBLG. The L_a mode above the G-band position for the bilayer is activated by intralayer electron–phonon scattering from the unfolded longitudinal optical phonon (LO) [56] branch. The measured L_a frequency of $1,621\text{ cm}^{-1}$ is consistent with the theoretical predictions [56] for a tBLG with $\theta \approx 7^\circ$. The LO dispersion is expected to have a non-monotonic dependence on the twist angle, with a maximum frequency at $\theta \approx 10^\circ$ but only slowly varying in the range of interest, thus making it unpractical to precisely determine the twist angle only from the Raman data.

We applied ultrafast TA microscopy to study the photo-physics of tBLG samples as function of the twist angle. A NIR pump pulse with photon energy E_{pump} is used to photo-excite the sample off-resonance with the vHs ($E_{\text{pump}} = 0.800\text{ eV}$ for stack 1 and $E_{\text{pump}} = 1.190\text{ eV}$ for stacks 2–3), while a second

tunable pulse, the probe, monitors the relaxation of the induced hot carriers' distributions as function of pump-probe time delay t . Pump and probe beams are collinearly coupled to a confocal microscope to achieve a $\approx 1\text{ }\mu\text{m}$ spatial resolution. The differential transmission ($\Delta T/T$) is measured as a function of the probe photon energy E_{probe} , using two distinct high sensitivity TA microscopes described in the Methods, guaranteeing a spectral coverage from 0.85 to 1.65 eV. Selected $\Delta T/T$ maps at fixed E_{probe} and time delay $t = 150\text{ fs}$ are reported in Fig. 2, for three tBLG stacks with different θ . As expected, the SLG regions exhibit a PB signal at all the investigated E_{probe} , detected as a positive $\Delta T/T$ signal. The PB signal shows a smooth monotone increase towards lower energy, following the momentum-spreading of the hot-carriers FD distribution.

This behavior contrasts to that of tBLG, for which a complex dependence on E_{probe} emerges shows also a PA signal. Specifically, under low photo-excitation fluences, we identified two characteristic components in the transient response: a clear peak in the PB and the appearance of PA band at lower energy. The PB peak corresponds to a factor 4–6 enhancement with respect to the SLG signal and it is centered in proximity to E_{vHs} (see first column of maps of Fig. 2). The PA is detected for $E_{\text{probe}} < E_{\text{vHs}}$. At lower probe photon energies, about 300 meV below E_{vHs} , the $\Delta T/T$ signal of tBLG becomes barely distinguishable from that of SLG. While a similar behavior is observed in all the investigated samples, the energy position of PB and PA bands changes with θ . The larger is the twist angle, the higher is E_{probe} at which similar tBLG/SLG contrast is observed. In stacks 2 and 3, bilayer regions with different twist angle are present, so that the signal intensity evolves differently according to their orientation.

For all samples, the precise value of the twist angle is determined by recording the hot-PLE spectrum. The experimental

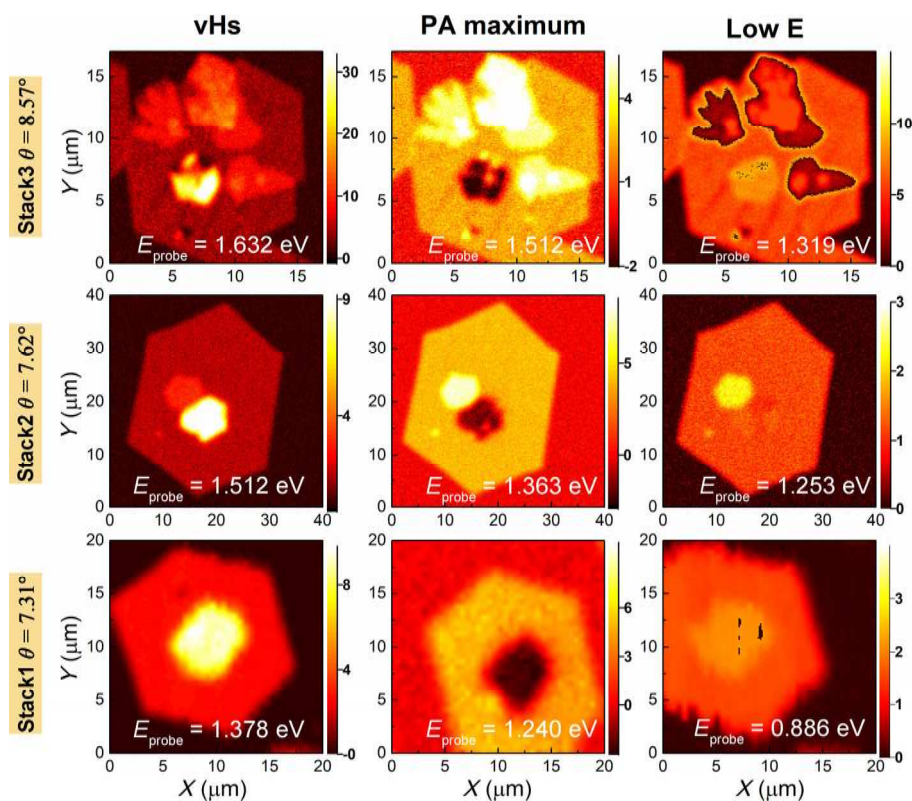


Figure 2 Color map images of the transient transmissivity $\Delta T/T$ (10^{-4}) at time delay $t = 0$, for three tBLG stacks with twist angle increasing from the lower to the upper row of panels: $\theta = 7.31^\circ$, 7.62° , and 8.57° . The probe energies for the first column of maps are taken in resonance with the vHs at $E_{\text{probe}} = 1.632$, 1.512 , and 1.378 eV ; for the second column at the maximum of the PA band at $E_{\text{probe}} = 1.512$, 1.363 , and 1.240 eV ; for the third column in resonance with the low-energy PB band at $E_{\text{probe}} = 1.319$, 1.253 , and 0.886 eV , as indicated in the panels.

$\Delta T/T$ spectra of monolayer and bilayer regions at $t = 150$ fs for several tBLG samples are reported in Fig. 3(a), together with the PLE spectra used to extract E_{vHs} and θ (blue symbols).

As θ decreases, the overall TA spectrum experiences a red-shift. The PLE peak almost overlaps with the PB peak, with the larger mismatch appearing in the stack with the most intense PA band. The signal near the vHs, indeed, results from the interplay of PA and PB contributions whose relative intensity varies with the twist angle and excitation fluence. Remarkably, the PA emerges at low photo-excited carrier densities of the order of $n = 1 \times 10^{13} \text{ cm}^{-2}$, as estimated from an incident fluence of $50 \mu\text{J}\cdot\text{cm}^{-2}$ considering 4% absorption. At an incident fluence of $350 \mu\text{J}\cdot\text{cm}^{-2}$, corresponding to $n = 7 \times 10^{13} \text{ cm}^{-2}$, the PA band disappears and a PB is observed over all the spectral range (see Figs. S2 and S3 in the ESM). The lack of previous evidences [47, 48] of contribution from the ISB to the TA of tBLG could be traced back to the higher absorbed photon flux attained by pumping resonantly to the vHs. This dominance of the PB over the PA for high laser fluence was also observed for the intra- and inter-band transitions in suspended single layer graphene [31].

The dependence of the experimental TA spectrum on crystal orientation is traced back to the modifications of the phonon modes, electronic structure and of the JDOS, in which we theoretically compute as a function of the twist angle and the hot-electron temperature T_e (see details in the Methods section) [57]. Figure 3(b) shows the calculated JDOS considering the interband and intersubband transitions between electronic states for the initial hot carrier temperature of 1,500 K and same twist angles as in Fig. 3(a). The electronic states populated by the pump pulse allow for the ISB transitions. The temperature of the quasi-equilibrium hot electron distribution is obtained considering a three temperature model [58] (see Figs. S4 and S5 and details in the ESM). The black (red) curves in Fig. 3(b)

show the JDOS for the interlayer ISB (interband-IB) transitions as a function of the twist angle θ . The ISB curves are calculated for the electron and hole transitions as indicated in Fig. 1(c) by the solid and dashed red arrows, respectively. The higher energy peak in the JDOS for ISB transitions corresponds to holes' excitations, while the lower-energy peak to the electrons. The difference in energy for the electron and hole ISB transitions is due to the small difference of their curvatures. Note that, for all the twist angles, the electron ISB peak appears about 50 meV below the IB peak due to the vHs transitions, while the hole ISB peak is almost overlapped with the vHs transitions (see Fig. S1 in the ESM). Figure 3(c) shows a comparison of both IB and ISB JDOS for carrier temperature of 1,500 K and room temperature (300 K); the blue arrows indicate that the ISB JDOS intensity increases with the temperature while the IB JDOS intensity decreases. The intensity of the JDOS is related to the dynamical conductivity (or absorption). In this way, the difference of the JDOS at these two temperatures is proportional to the $\Delta T/T$ spectrum and qualitatively explains the opposite sign of the contributions from ISB and IB transitions to the TA signal.

The increase of the JDOS associated to ISB transitions due to photo-excitation corresponds to the PA signal observed at energies just below E_{vHs} in the experimental data of Fig. 3(a). The ISB peak for holes is very close to the E_{vHs} transition that dominates the $\Delta T/T$ signal at these energies. The strong angle dependence of the PA energy position results in ~ 250 meV tuning with only a $\sim 1.26^\circ$ twist angle change. Model predictions of the PA energy position based on the JDOS calculation, with the folding method, agree very well with the experimental data. In the ESM, the expected values for a large range of twist angles (from 0° to 30°) are reported in Fig. S1 in the ESM and appear always slightly red-shifted with respect to the vHs transition.

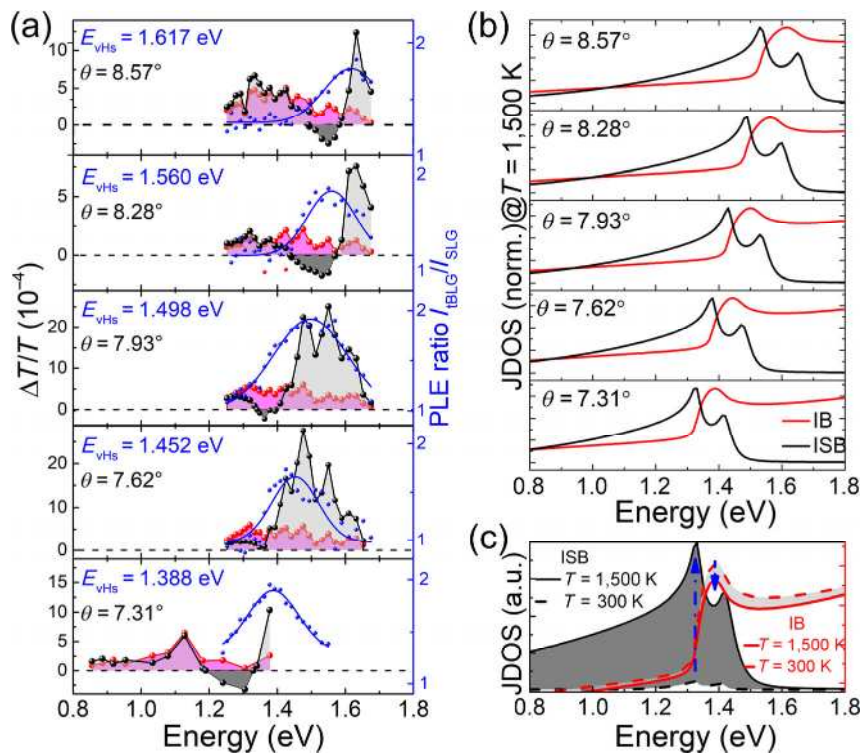


Figure 3 (a) Transient transmissivity spectra of SLG (red-dot and solid line) and tBLG (black-dot and solid line) at fixed time delay $t = 150$ fs for samples with different θ as indicated by the labels. The blue dots are the PLE intensity ratio of the tBLG to the SLG fitted with a Gaussian function (blue solid line) peaked at E_{vHs} . (b) Calculated JDOS for the ISB transition (black) and the E_{vHs} transition (red) for a hot electron temperature of 1,500 K. (c) A comparison of the IB and ISB JDOS for 1,500 K and the room temperature 300 K. The difference of the JDOS at these two temperature is proportional to the $\Delta T/T$ spectrum.

Figure 4 reports the $\Delta T/T$ dynamics of stack 1. A similar relaxation scenario is observed for all the stacks, once the shift of energy position of the transient spectrum is taken into account (see Fig. S6 in the ESM). The recovery dynamics of tBLG is consistently different from that of SLG. The dynamics of tBLG (full colored dots) is compared to that of SLG (open black symbols) for E_{probe} corresponding to the main features of the optical response: the PB peak at the vHs, the PA corresponding to ISB transitions and the low-energy PB band. The $\Delta T/T$ dynamics in SLG is energy-independent and it is described by a bi-exponential decay convoluted to an instrumental response function (IRF) of ≈ 120 fs. The extracted time constants are $\tau_1^{\text{SLG}} = 120 \pm 20$ fs and $\tau_2^{\text{SLG}} = 1,980 \pm 60$ fs. These values are characteristic of SLG samples with low defect density [43]. The transient transmissivity depends superlinearly on T_e through the FD distribution function, so that the time evolution of T_e and $\Delta T/T$ are not correlated in time. However, while the fast relaxation component is strongly influenced by the superlinearity, the slow relaxation component of transient transmissivity is generally assumed as a reliable estimation of cooling time via anharmonic coupling of the thermalized bath of hot electrons and SCOPs with the acoustic phonons [59]. The $\Delta T/T(t)$ dynamics of tBLG, on the contrary, strongly depends on the transition energy even though, away from the PA and the vHs, it is very similar to that of SLG. At the vHs, the PB not only has a much higher initial intensity than for SLG, but it decays on a longer time scale. The dynamics, after deconvolution with the IRF, is best fit by a biexponential decay with $\tau_1^{\text{tBLG}} = 140 \pm 20$ fs and $\tau_2^{\text{tBLG}} = 2,500 \pm 100$ fs. The PA band is best described by a three-exponential decay with time constants $\tau_1^{\text{tBLG}} = 120 \pm 30$ fs, $\tau_2^{\text{tBLG}} = 1,960 \pm 40$ fs and $\tau_3^{\text{tBLG}} = 70 \pm 2$ ps with the additional decay component responsible for the tail extended to 100 ps in Fig. 4(b). Such long lifetimes can be explained by the peculiar temperature dependence of the JDOS that emerges at finite twist angles. We modeled the

decay curves by the ratio of the calculated JDOS as a function of the electron temperature T_e (Figs. 4(c) and 4(d)). We calculated the time evolution of T_e from a three temperature model, considering the electron energy relaxation through strongly coupled and weakly coupled phonon modes [58]. The specific heats for the electrons, SCOPs and weakly coupled phonons are obtained considering their density of states from tight-binding [57, 60] and force constant [61] methods parameterized by first principles calculations. For tBLG, it is important to include the additional low frequency and high density phonon modes at the Γ point, that are not present in SLG, as representing the out-of-plane breathing of adjacent layers interacting via weak van der Waals forces (details in the ESM). The calculated $\Delta T/T(t)$ dynamics, both at the vHs transition and at the ISB transition, reproduces very well the experimental results. This indicates that the density of states enhancement at the vHs and the changes in the electron and phonon heat capacities can explain the observed long decay of the PA and PB bands.

To conclude, we demonstrated that at low excited carrier density the transient optical response of tBLG shows two peaks, one due to photoinduced absorption from intersubband transitions and another one due to photobleaching of the interband transitions in resonance with the vHs (E_{vHs}). Similar to the vHs, the energy positions of these peaks can be controlled with the twist angle. At the vHs, we observed a carrier cooling time which is about 30% longer than for SLG, while the photoinduced intersubband signal shows a long-living tail up to 100 ps. A simple model, based on the JDOS enhancement and on the evolution of the electronic temperature as the hot electrons equilibrate with the tBLG phonon modes, explains well the experimental TA signal, both for the peaks position and for their temporal decays, without recurring to more complex multiparticle excitations as bound excitons or non-linear processes such as two-photon absorption.

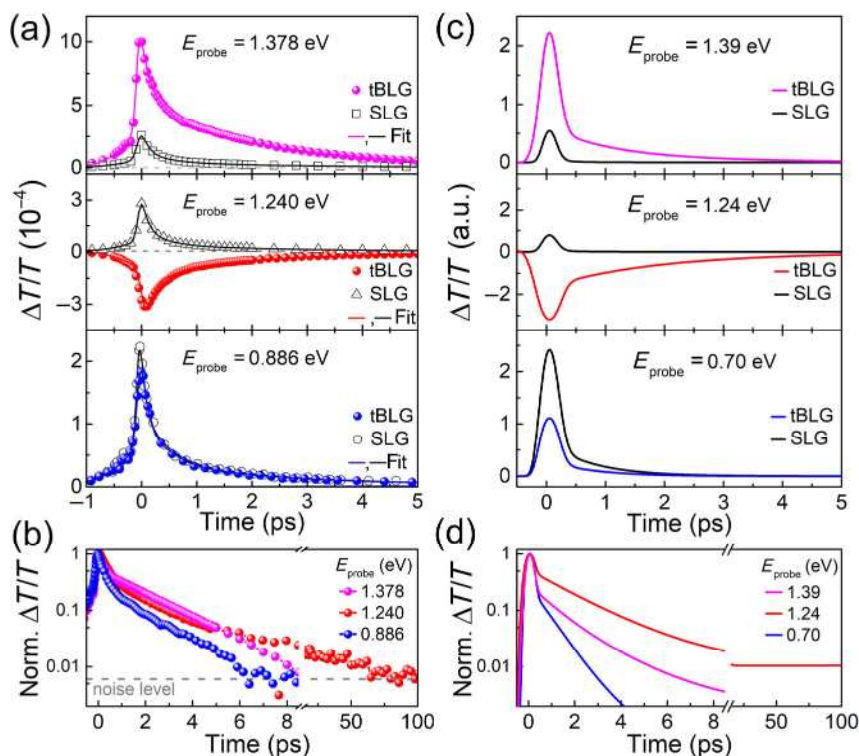


Figure 4 (a) $\Delta T/T$ dynamics of tBLG (full colored dots) and SLG (open black symbols) for the stack with $\theta = 7.31^\circ$ at probe energy $E_{\text{probe}} = 1.378$ eV corresponding to E_{vHs} , 1.240 eV corresponding to the ISB; 0.866 eV in the low-energy PB band $E < E_{\text{ISB}}$. (b) Comparison of $\Delta T/T(t)$ normalised to the maximum over an extended time scale. (c) Theoretically estimated decay curves based on the electron temperature time decay. In the simulations we used $E_{\text{probe}} = 1.39$, 1.24 and 0.70 eV to best reproduce the experimental decay behavior. (d) Normalised theoretical curves obtained in (c).

Methods

Sample preparation and characterization The twisted bilayer graphene single crystals were prepared by ambient pressure chemical vapor deposition (AP-CVD) synthesis on polycrystalline Cu foils. The nucleation conditions on Cu foils are controlled to allow both constituent layers to form as hexagonal single crystals, and each tBLG grain has a specific twist angle. The samples were transferred to a transparent amorphous quartz substrate for the optical images and spectroscopy measurements. More details about the sample preparation are presented in Ref. [62].

To select the samples for TA studies we first measured the sample twist angle by an analysis of the flake shapes on optical microscopy white light images. The optical images were obtained using an Olympus microscope (DP72) in reflection mode with a 100× objective lens. To obtain the twist angle we drew a hexagon for each layer and measured the angle between the edges of the two hexagons [52], as can be seen for the sample in Fig. 1(d).

We also characterized the sample twist angle by Raman spectroscopy using an alpha300R WITec confocal Raman spectrometer at excitation energy of 1.96 eV (633 nm). The Raman spectra were measured in backscattering geometry on a triple monochromator spectrometer equipped with a liquid-N₂ CCD. All measurements were performed at room temperature.

For the PLE measurements a PL image was acquired for each excitation laser energy, that was tuned to cover the range of the vHs transition for each sample. The PL intensity was averaged at the bilayer region and divided by the PL at the monolayer region to obtain each point in the PLE spectra. The PL signal was measured in back scattering, separated from the excitation laser by a dichroic mirror (Semrock FF665-Di02). A bandpass filter (75 nm centred at 610 nm) was used in front of the detector to further block any scattered laser light (Chroma 610/75M).

High-sensitivity TA microscopy The TA data here reported have been acquired using two distinct microscopes working in complementary probe energy ranges, enabling an overall spectral coverage of 1 eV. The microscope used for the probe energy range of 0.8–1.4 eV was based on a Er-doped fiber laser (Toptica-Femtofiber pro) generating 300 mW, 150 fs pulses centered at 1,550 nm with 40 MHz repetition rate. A portion of the output of the laser was used as the pump pulse tuned to 0.8 eV and was modulated with an acousto-optic modulator operating at 1 MHz. The probe pulse extending from 0.73 to 1.45 eV was obtained by super continuum (SC) generation from the laser fundamental focused in a highly-nonlinear fiber. The low-energy branch of the SC and the fundamental were filtered out with a short pass filter cutting at 1,500 nm. The pump and the probe beams were collinearly focused on the sample with an objective (Olympus-LCPLN-IR with magnification 100× and NA = 0.85) to a spot size of about 1 μm. The probe transmitted by the sample was collected with an 8 mm focal length achromatic doublet, spectrally filtered with a monochromator with 5 nm resolution and detected by an InGaAs amplified photodiode with 4 MHz bandwidth. The TA signal was measured with a lock-in amplifier with 300 ms effective time constant, resulting in a $\Delta T/T$ sensitivity of 10^{-7} . TA dynamics was monitored by changing the pump-probe delay with an optical delay line, while the TA maps (images) at fixed probe photon energy and time delay were acquired by moving the sample with a motorized three-axis piezo-stack linear stage (Newport NPXYZ100).

The microscope used for the probe energy range of 1.25–1.65 eV was based on a commercial femtosecond optical parametric oscillator (OPO, Insight DS+, Newport, CA, USA) used as the laser source, with the fundamental 1,040 nm (1.1923 eV) beam as the pump and the tunable output 750–990 nm (1.252–1.653 eV) as the probe. The pump beam was modulated at 20 MHz by an electro-optical modulator, collinearly combined with the probe beam and delivered into a laser-scanning microscope (FV1200, Olympus). The laser beams were focused onto the sample with an air objective (UPLSAPO 20×, NA = 0.75, Olympus) to about 1.5 μm diameter, raster scanned by a pair of galvo mirrors, transmitted through the sample, passed through an optical filter to block the pump beam, and then directed onto a large-area silicon photodiode. Pump fluence was kept at approximately $50 \mu\text{J}\cdot\text{cm}^{-2}$ (2×10^{14} incident photons/cm²). The pump and probe beams were combined with a dichroic mirror (DMSP1000, Thorlabs) and aligned collinearly. The probe beam was optically filtered by two short-pass filters (FF011010/SP-25, Semrock), collected by a photodiode, and demodulated with a commercial lock-in amplifier (HF2LI, Zurich Instruments) to extract the TA signal. A pixel dwell time of 2 μs and image size of 320 × 320 pixels were used in the experiments. The cross-correlation between pump and probe pulses at the sample was measured to be ~ 0.3 ps, and the time delay interval between adjacent images was set to $\Delta t = 133$ fs. A single t scan of 20 ps took about 1.5 min, and a complete spectral scan took about 30 min.

Theoretical model The electronic structures were obtained by folding the SLG calculation results. For SLG, we followed the procedure given in Refs. [57, 60], where the electronic structure calculations were based on a fifth neighbors tight-binding approach, with one orthonormalized p_z orbital per site, in which the hopping parameters were fitted to reproduce density functional theory (DFT) calculations with many-body corrections.

The electronic transitions between bands in tBLG were captured considering two SLG BZs twisted by a certain angle θ . In this way, we considered only four electronic bands for the tBLG, one valence and one conduction band for each layer. For low temperatures, only the electronic IB transitions are possible. The magenta arrow in Fig. 1(c) shows the IB transition at the vHs, that gives rise to a peak in the JDOS at an energy E_{vHs} which is a function of θ . When the temperature increases, ISB transitions between valence, or between conduction bands, are also possible (red arrows in Fig. 1(c)).

The allowed IB and ISB transitions do not depend on the size of the minigap, which appears due to the hybridization of the eigenstates near the band intersections. Our model cannot reproduce the interaction between layers and the atomic relaxation is not taken into account. However, Havener et al. [19] have shown that, although the interlayer interactions perturb the bands from each layer producing minigaps, which splits the valence and the conduction bands in tBLG, the difference in energy between the minigaps is generally too small to be seen directly in the PL and absorption spectra, contributing only to the peak broadening. Also, since the allowed electronic transitions do not depend on the size of the minigap and the PL peak is usually symmetric, which means that both transitions from minigaps to the conduction and the valence bands contribute equally, the energy position of the JDOS peak obtained by the folding approach is supposed to give a good estimation of the twist angle. This justifies the folding approach used in our simulations, which does not consider interaction between layers [19, 56].

In our model, it is possible to analyze the JDOS for IB and ISB transitions separately, as a function of the electronic temperature. We computed the JDOS as

$$J(T_e, E) = \frac{\gamma}{\pi N_k} \sum_{i,j,k} \frac{f(E_{i,k}, T_e) - f(E_{j,k}, T_e)}{(E_{i,k} - E_{j,k} + E)^2 + \gamma^2} \quad (1)$$

where the sum is performed on a uniform grid of $N_k = 2,400 \times 2,400$ k-points over the two dimensional BZ and for the different pairs of bands i, j while $\gamma = 1 \times 10^{-2}$ eV is a small energy broadening parameter related to the inverse of the electron-hole lifetime. The function $f(E_{i,k}, T_e) = [1 + \exp(E_{i,k}/T_e)]^{-1}$ is the Fermi function for a specific band energy i of the state k and temperature T_e (the chemical potential μ is close to the Fermi level and both are set to zero).

Using only IB transitions in the JDOS calculation we found the energy peaks corresponding to the E_{vHs} for a specific twist angle θ . For the same values of E_{vHs} obtained by the PLE peaks, we computed the normalized JDOS for IB and ISB transitions, as a function of the probe energy for $T_e = 1,500$ K, which is the estimated temperature for the hot electrons excited by the pump laser (see Figs. S4 and S5 in the ESM). We saw that the peaks corresponding to ISB transitions are always at lower energies than the IB transitions between the vHs, as shown in Fig. 3(c).

An estimation of the $\Delta T/T$ dynamics can be obtained assuming that electron-radiation matrix element is constant for all transitions. In this way, the dynamical conductivity σ (or absorption α) becomes proportional to the JDOS which we computed including both the IB and the ISB as function of T_e . Details of the T_e time-evolution calculation are described in the ESM.

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