



Analytic roughness prediction by deep rolling

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Abstract

Deep rolling is a widely applied mechanical surface and subsurface treatment method. It is typically used after conventional machining to improve the roughness, increase the surface hardness and to induce compressive residual stresses. The main influence parameters on the surface topography are the applied deep rolling pressure, the ball diameter and the feed. In general, low feeds, larger ball diameters and higher pressures result in an even surface finish. However, an exact prediction of the roughness is not possible. Therefore, it is the aim of the presented research to find a generally applicable method for surface roughness prediction after deep rolling for a variety of steel and aluminum materials. It is shown that the surface topography can be predicted by an analytical model with high accuracy.

Keywords Deep rolling · Roughness · Surface topography · Roller burnishing

List of symbols

d_b	Ball diameter (mm)
E	Unified Young's modulus (GPa)
f	Feed (mm)
F_w	Deep rolling force (N)
h_d	Peak distance (mm)
h_r	Peak height (mm)
p_{max}	Contact stress (MPa)
p_w	Deep rolling pressure (MPa)
Q_{def}	Stress ratio $p_{max}/R_{p0.2}$ (–)
r	Unified radius (mm)
r_c	Contact radius (mm)
r_e	Cutting edge radius (mm)
$R_{p0.2}$	Yield strength (MPa)
u	Overlap factor (–)
v_r	Rolling speed (m/min)

η	Efficiency coefficient (–)
ρ	Density (g/cm^3)

1 Introduction

The surface topography plays a vital role for the functional behavior of metallic components. To guarantee the desired functionality of a component, it is often necessary to achieve a certain surface quality in form of a certain roughness. The manufacturing process deep rolling or roller burnishing, which is usually applied as a finishing process after cutting processes, offers the possibility for the surface quality improvement. A general observation is that deep rolling flattens the cutting-induced roughness peaks and that the roughness decreases using smaller feeds or higher ball diameters. One common method to describe the mechanical load applied by the deep rolling tool is the contact theory by Hertz [1]. Here, the contact stress during elastic deformation is considered. The following assumptions are common for the description of load stresses during deep rolling: Only elastic deformation, contact between two spherical objects [1]. The latter can be calculated for the more realistic contact case of a cylinder-sphere contact as performed by Maiß [2], but these adjustments results in minor and therefore negligible changes regarding the contact diameter. The calculation starts with an estimation of the deep rolling force F_w , which relates the deep rolling pressure p_w to the contact area of half of the sphere:

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$$F_w = p_w \cdot \left(\frac{d_b}{2}\right)^2 \cdot \pi \cdot \eta \quad (1)$$

η is the efficiency coefficient, which can be assumed as $\eta = 0.8$ as observed by Denkena et al. [3]. The contact radius r_c is calculated by:

$$r_c = \sqrt[3]{\frac{3 \cdot (1 - \nu) \cdot r \cdot F_w}{2 \cdot E}} \quad (2)$$

where E is the unified Young's modulus and R the unified radius:

$$p_{max} = \frac{1}{\pi} \cdot \sqrt[3]{\frac{1.5 \cdot F_w}{r_c^2} \cdot \left(\frac{E}{1 - \nu^2}\right)^2} \quad (3)$$

According to Klocke and Mader [4], the overlap factor u has a high influence on different surface values. The overlap u is a unitless factor, which relates the feed f_w to the contact radius.

$$u = 1 - \frac{f}{r_c} \quad (4)$$

Klocke [5] reports a reduction of 30–50% on the peak-to-valley height R_z machining quenched AISI52100 with a hardness of 62 HRC using a deep rolling tool $d_b = 6.35$ mm. Here, a flattening of peaks with no full surface deformation was observed. A similar result is achieved by Grzesik and Zak [6], who observed a roughness reduction after applying a deep rolling process to hard turned SAE5140, where remains of the turning induced profile are visible after the deep rolling process. Bouzid et al. [7] provide an analytic solution for the calculation of the resulting roughness after grinding and turning pre-treatments, which can play a role regarding the resulting surface after deep rolling. The initial topography is taken into account. Bouzid et al. [7] also observe no total deformation of the surface and roughness peaks of the pre-treatment are observable on the deep rolled surface. The results of Bouzid et al. and Grzesik contradict investigations on different materials as performed by Li et al. [8] for two different aluminum grades. According to Li, depending on the feed and therefore the resulting overlap between each reversion, a total deformation induces the flattening of all initial roughness peaks. A possible reason for these different outcomes lies in differences in material and a load induced plastic deformations. Therefore, Li et al. consider the plastic deformation and achieve a higher agreement between predicted and machined roughness. All of the mentioned methods provide solutions for the used materials but lack a general explanation for different materials. It also remains unclear, if the prognosis of the surface topography can be performed with or without consideration of the initial workpiece topography. Therefore, this paper aims to find

Table 1 Material properties

Parameter	Material		
	Al6082	AISI1045	AISI4140
Density ρ	2.83 g/cm ³	7.83 g/cm ³	7.72 g/cm ³
Young's modulus E	69 GPa	210 GPa	210 GPa
Hardness	158 HV1	302 HV1	515 HV1
Yield Strength $R_{p0.2}$	260 MPa	800 MPa	1,350 MPa

Table 2 Parameters for the turning operations prior to the deep rolling process

Parameter	Material		
	Al6082	AISI1045	AISI4140
Cutting depth a_p	0.4 mm	0.3 mm	0.65 mm
Feed f	0.1 mm	0.1 mm	0.1 mm
Cutting speed v_c	280 m/min	280 m/min	400 m/min

a general analytical solution for the prediction of surface topographies after deep rolling. To create a solution, different materials are machined under variation of various process parameters. In comparison to the mentioned sources, the approach in this paper is to machine a variety of materials with different mechanical properties with a broad parameter variation.

2 Experimental setup

To investigate the influence of the deep rolling parameters on the surface topography, two sets of experiments were performed. While the first experimental stage aimed for a general analysis of the surface topography and the generation of a modelling method, the second stage aimed to evaluate the limitations of said method. To cover a wide range of materials, the experiments were performed using the steels AISI1045, AISI4140 and the aluminum alloy Al6082 T5. The steels have been annealed to different hardness states. While the AISI4140 was quenched and tempered to 515 HV1, the AISI1045 was quenched to 302 HV1. The material properties are listed in Table 1. The yield strength was calculated according to Pavlina and van Tyne [9].

Prior to the deep rolling experiments, the samples were turned using Walter SNMA120408-RK5 cutting inserts. The parameters are listed in Table 2. The experiments were conducted on a Gildemeister CTX 520 lathe using hydrostatic ECOROLL tools with HG3 (ball diameter $d_b = 3.175$ mm), HG6 ($d_b = 6.35$ mm) and HG13 ($d_b = 12.7$ mm) tools with an adjustable compressor, which provides deep rolling pressures between $p_w = 2 - 60$ MPa. The forces

were measured using a Kistler 9121 dynamometer. The surfaces were analyzed using a Mahr MarSurf LD 130 Perthometer.

In the first experimental stage, the workpieces were deep rolled using three different ball diameters d_b and overlap factors u . To ensure a similar load and level of deformation, the maximum Hertzian pressure p_{max} was set in uniform relation to the yield strength $R_{p0.2}$. This deformation ratio is defined as:

$$Q_{def} = \frac{p_{max}}{R_{p0.2}} \tag{5}$$

The calculation of the overlap factor u and p_{max} was performed according to Eqs. 1 to 4. The parameter variation is depicted in Table 3. The resulting machining parameters for each experiment are depicted in Table 4.

The second set of experiments was performed afterwards to investigate limitations of the resulting analytical model. The ball diameter was set to a constant value of $d_b = 6.35$ mm and the feed f was varied between $f = 0.05$ mm and $f = 0.8$ mm. The deep rolling pressure was varied in three stages for each material in order to induce different levels of deformation. The stress ratio Q_{def} was taken to account in order to ensure a similar deformation on the different materials. Here, the limitations of the pump system regarding the deep rolling pressure p_w range should be noted. The parameters for the second set of experiments are depicted in Table 5. As a result of said limitations, even lower p_w -values

Table 3 Parameters used for the first set of experiments

Parameter	Unit	Variation		
		–	0	+
Ball diameter d_b	mm	3.175	6.35	12.7
Overlap factor u	%	– 75	50	80
Contact stress p_{max}	MPa	$7 \cdot R_{p0.2}$		
Rolling speed v_r	m/min	100		

Table 4 Parameters used for the first experimental stage

	Rolling pressure	Feed	Ball diameter	Overlap factor	Max. Hertzian stress	Stress ratio
	MPa	mm	mm	–	MPa	–
AISI1045	16	0.48	3.175	– 0.75	5890	7.36
		0.14		0.5		
		0.05		0.8		
	14	0.91	6.35	– 0.75	5911	7.39
		0.26		0.5		
		0.1		0.8		
	12	1.74	12.7	– 0.75	5908	7.39
		0.5		0.5		
		0.05		0.8		
AISI4140	56	0.32	3.175	– 0.75	8981	6.65
		0.09		0.5		
		0.04		0.8		
	51	0.6	6.35	– 0.75	9013	6.68
		0.17		0.5		
		0.07		0.8		
	41	1.14	12.7	– 0.75	9009	6.67
		0.33		0.5		
		0.2		0.8		
Al6082	3	0.25	3.175	– 0.75	1953	7.52
		0.07		0.5		
		0.03		0.8		
	2.8	0.47	6.35	– 0.75	1959	7.53
		0.13		0.5		
		0.05		0.8		
	2	0.87	12.7	0.75	1937	7.45
		0.25		0.5		
		0.05		0.8		

Table 5 Parameters used for the second experimental stage

	Rolling pressure	Feed	Ball diameter	Max. Hertzain stress	Stress ratio
	p_w	f	d_b	p_{max}	Q_{def}
	MPa	mm	mm	MPa	–
AISI1045	7	0.05–0.8	6.35	4624	5.78
	14			5824	7.28
	40			8264	10.33
AISI4140	30	0.05–0.8	6.35	7506	5.56
	40			8264	6.12
	50			8896	6.59
Al6068	2	0.05–0.8	6.35	1731	6.66
	5			2340	9
	7.5			2678	10.3

lead to a higher Q_{def} for Al6082 than for AISI4140. Therefore, a lower deformation can be expected for the machined AISI4140.

3 Results and discussion

Figure 1 depicts the tactile measurement of deep rolled AISI1045 samples with the usage of three different overlap factors ($u = -75\%$, $u = 50\%$, $u = 80\%$). Also depicted is the turned surface to visualize the difference between the turned and the deep rolled surface. The tool diameter was $d_b = 3.175$ mm. On the left hand side, the turned surface is indicated by the typical periodic cutting profile. In the center, the first contact position between deep rolling ball and workpiece is visible. Because of the toolpath, which provides a linear feed into the contact position with the hydrostatic pressure already attached, there is a deeper groove compared to the following position. The upper graph shows the negative overlap of $u = -75\%$. This means that no section of material comes into double contact with the workpiece. The underlying principle of volume constancy in forming processes results in a high penetration depth and width. Also visible are the peaks induced by the previous turning operation. This part of the material is not deformed and the roughness peaks are not flattened.

Figure 2 shows the deep rolled part of the AISI1045 samples. Here, the full variation of ball diameters using the different overlap factors is shown. For each ball diameter, using the overlap factor of $u = -75\%$, roughness peaks from the previous turning operation are visible. With increasing ball diameter and consistent pressure, a higher penetration depth and width is visible because of the higher process forces. This this results in a higher necessary feed f to achieve the overlap factors. Using the overlap factor of $u = 50\%$, the profile is periodic with each ball diameter. Because of the larger ball diameter d_b and

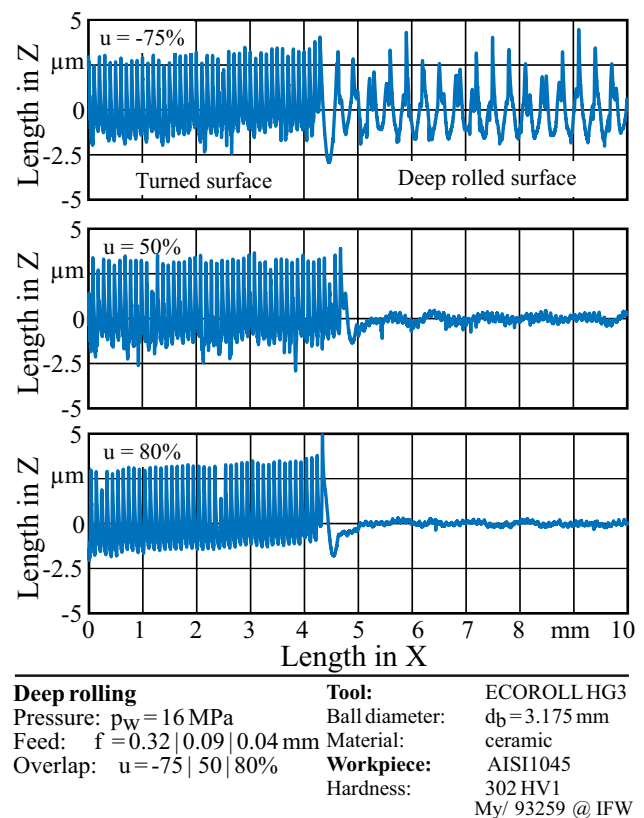


Fig. 1 Surface topography after turning and subsequent deep rolling of AISI1045

the increasing feed f to achieve the same overlap factor, the distance between the peaks increases. The surface after a deep rolling procedure under the usage of an overlap factor of $u = 80\%$ does not show periodicity. The visual representation does not allow a statement about peak height or distance distribution. It is also visible, that a similar roughness R_z occurs regardless of the ball diameter (Fig. 3). The resulting profiles from the deep rolling of

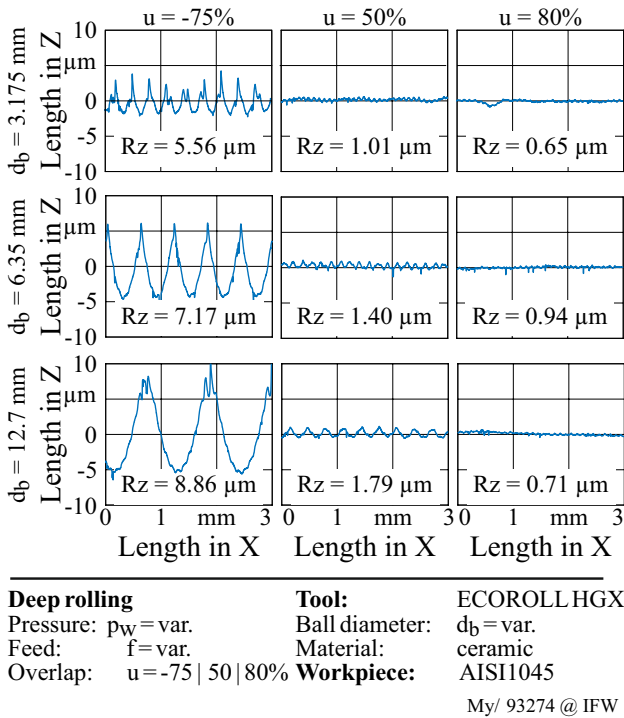


Fig. 2 Development of the surface topography on AISI1045 with alternating overlaps and ball diameters

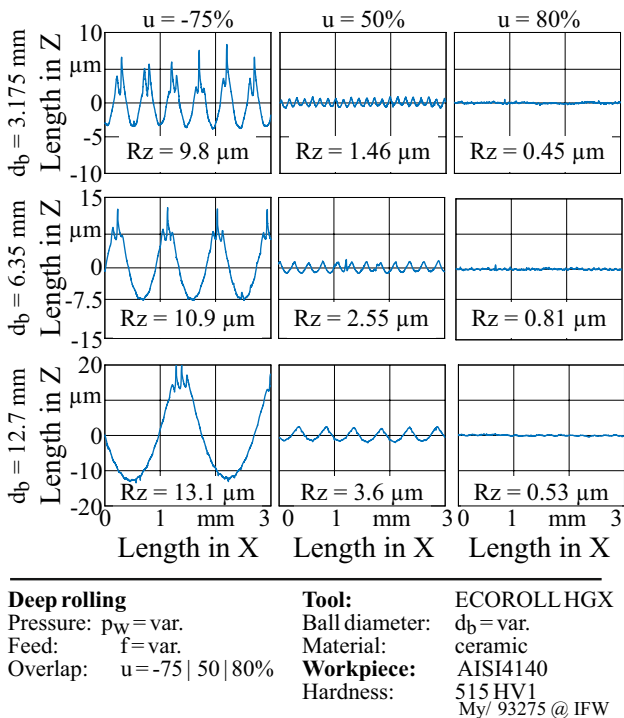


Fig. 3 Development of the surface topography on AISI1410 with alternating overlaps and ball diameters

the Al6082 samples look slightly different, as displayed in Fig. 4. While the resulting surface using an overlap factor of $u = -75\%$ for the ball diameters $d_b = 6.35 \text{ mm}$ and $d_b = 12.7 \text{ mm}$ looks similar to those on the AISI1045 and AISI4140 samples, $d_b = 3.175 \text{ mm}$ does not create such a clear periodic profile with visible turning peaks. This behavior can be explained by the comparably small feed f which is necessary to achieve an overlap of $u = -75\%$. The surface profiles for $u = 50\%$ are also periodically distributed and show a line of round indentations, while $u = 80\%$ creates a smooth surface with no obvious periodic characteristic. These results indicate that independent of the plastic material behavior, a higher overlap factor and a larger ball diameter d_b leads to a smoother surface, which is also a general conclusion of the state of the art. It can also be seen, that both, deep rolled and turned surfaces have seemingly periodically distributed peaks. In the case of a negative overlap factor u , the remaining peaks from turning process are between the grooves from deep rolling.

A similar behavior can be seen for the same treatment applied to the AISI4140. Using the negative overlap factor $u = -75\%$, the round indentations are intermitted by the peaks created by the turning process. The profile created using overlap of $u = 50\%$ is also periodic. The profile created using $u = 80\%$ does not display an obviously periodic profile and similar roughness values R_z .

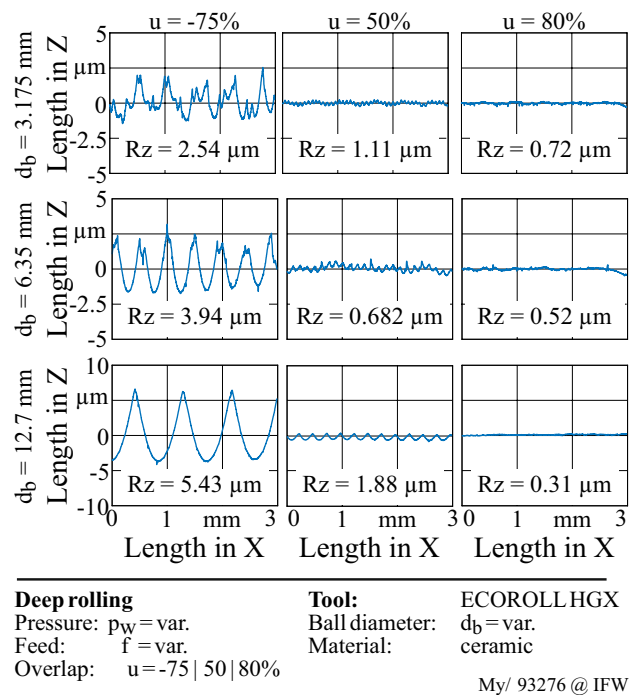


Fig. 4 Development of the surface topography on Al6082 with alternating overlaps and ball diameters

4 Analytic model

Because some of the surfaces generated by deep rolling showed a periodic profile with round indentations, the measurements were analyzed using a Fast Fourier Transformation (FFT) algorithm to find links between the manufacturing process and the resulting surface. Figure 5 shows the resulting surface topographies and the Fourier transformations for Al6082 with an ECOROLL HG13 deep rolling tool. For the overlap factors $u = -75\%$ and $u = 50\%$, the reciprocal of the dominant wavelength x_{max} is equal to the feed f set during the deep rolling process. This correlation is not discernible with an overlap factor of $u = 80\%$. A possible explanation may be a material pile up which results from plastic deformation in combination with the close iterations resulting from the feed f . The congruence between a ball geometry and the surface is also shown.

Here, the spherical contour is elliptically represented by the length distortion between the axes. The good optical fit for the overlap factors $u = -75\%$ and $u = 50\%$ shows that the generated surface is a repeated pattern of nearly spherical indentation. The deviation between ball contour

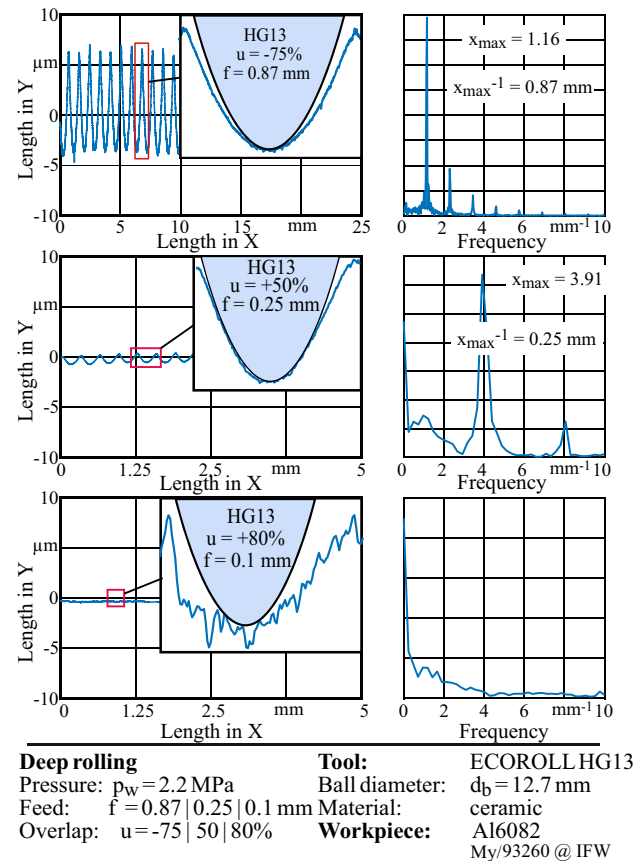


Fig. 5 Periodic representation of the feed in deep rolled surfaces

and the indentation may result from elastic springback, and the remaining surface is plastically deformed. With regard to those results, the resulting surface for the overlap of $u = 50\%$ can be described by the indentation geometry of the tool. The Fourier analysis showed that the impressions are formed at regular intervals corresponding to the feed rate for $u = -75\%$ and $u = 50\%$. A reproduction of the surface using ball diameter d_b and feed f is however only possible for $u = 50\%$, because a negative overlap leads to undeformed peaks in between the spherical profiles. Regardless of material or d_b , the surface for $u = 50\%$ can be simulated using an intersection of spheres which are aligned in the distance of the feed f . As an example, and proof of concept, Fig. 6 shows a comparison between the deep rolled surface and a surface generated by the above mentioned method implemented in a Matlab model. To describe the height of the peaks for applicable process parameters, a simple geometrical model, comparable to the calculation of the theoretical roughness during turning can be used. This procedure is described in Eqs. 6 and 7. To calculate the peak height h_r , the first step is to calculate the difference h_d between the ball radius $d_b/2$ and h_r . This is performed using the Pythagorean theorem

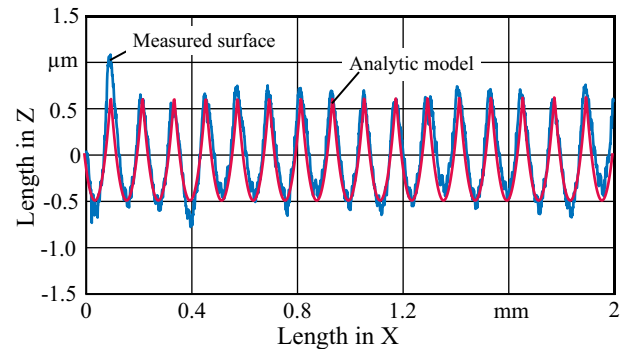


Fig. 6 Analytic model for the deep rolling of quenched AISI4140

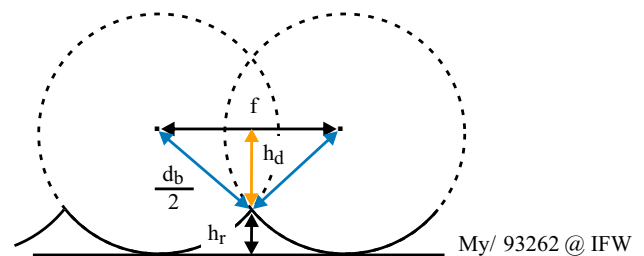


Fig. 7 Calculation of the peak height

for the two same-sized right-angled triangles between both center points and the intersection of both spheres (Fig. 7).

$$h_d = \sqrt{\left(\frac{d_b}{2}\right)^2 - \left(\frac{f}{2}\right)^2} \tag{6}$$

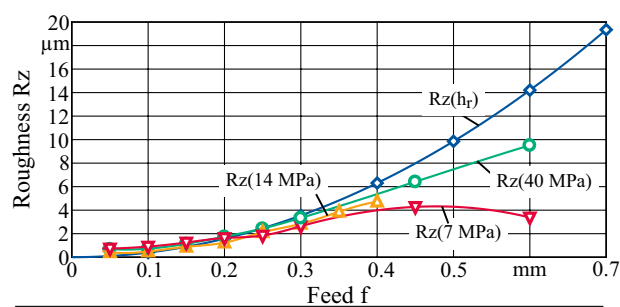
$$h_r = \frac{d_b}{2} - h_d = \frac{d_b}{2} - \sqrt{\left(\frac{d_b}{2}\right)^2 - \left(\frac{f}{2}\right)^2} \tag{7}$$

The first set of experiments showed a possibility to determine the resulting surface after a deep rolling process. The experiments showed that the surfaces with an overlap factor of $u = 50\%$ are well predictable using this simple geometric relationship. The description of a negative overlap is not possible because some parts of the surface are not in contact with the tool and therefore not plastically deformed. This results in a helical groove track around the workpiece. A possible limit could lie in the pressure and therefore the resulting ratio Q_{def} . On the observed workpieces, the applied pressure p_w provides sufficient deformation in a nearly spherical area, which is greater in comparison to the feed. In order to investigate the influence of the pressure p_w and to investigate a suitable feed range, the next chapter focusses on a broader parameter variation in order to verify this model.

5 Experimental verification of the model

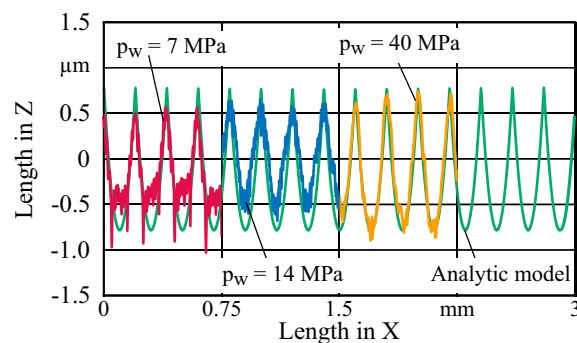
The first chapters demonstrate promising results regarding the description of the surface topography after deep rolling with overlap factors, calculated following the Hertzian contact theory of $u = 50\%$. To find the limitations of the mentioned approach, all three materials were again turned and deep rolled using the parameters described in Table 5. In order to provoke different levels of plastic deformation, the deep rolling pressure p_w was varied in three stages with alternating feeds.

The resulting surfaces were analyzed regarding the Roughness Rz and compared with the analytically calculated surfaces. Figure 8 shows the comparison for AISI1045. The x-axis represents the feed and the y-axis the Roughness Rz . Rz was determined by an analysis of an analytically calculated surface created with the above mentioned method. For the machining of AISI1045, pressures of $p_w = 7$ MPa, 14 MPa and 40 MPa were used. An accordance of 76% between the geometric model and the measured roughness is calculated for feed rates between $f = 0.05$ – 0.3 mm. By using a higher feed, the difference between the analytical roughness and the experimentally obtained profile increases with lower pressures. This behavior is illustrated in Fig. 9 for a feed of $f = 0.2$ mm.



Deep rolling	Tool:	ECOROLL HG6
Pressure: $p_w = \text{var.}$	Ball diameter: $d_b = 6.35$ mm	
Feed: $f = \text{var.}$	Material: ceramic	
Overlap: $u = \text{var.}$	Workpiece:	AISI1045
	Hardness:	302 HV1 My/93263a@ IFW

Fig. 8 Theoretical vs. experimental roughness for AISI1045



Deep rolling	Tool:	ECOROLL HG6
Pressure: $p_w = \text{var.}$	Ball diameter: $d_b = 6.35$ mm	
Feed: $f = 0.2$ mm	Material: ceramic	
Overlap: $u = \text{var.}$	Workpiece:	AISI1045
	Hardness:	302 HV1 My/93279 @ IFW

Fig. 9 Surfaces after deep rolling with alternating pressures p_w

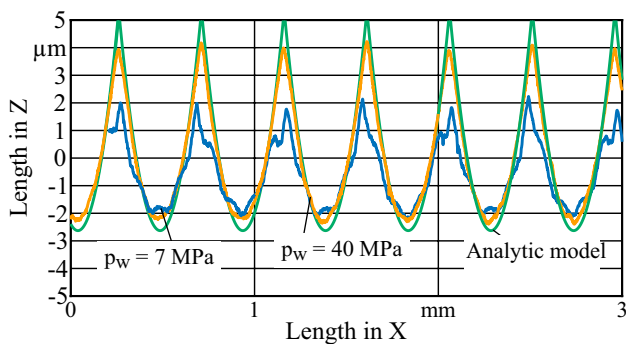
The first segment focusses on the surface generated by the rolling pressure $p_w = 7$ MPa and $Q_{def} = 5.78$. Here, a distortion is visible on the bottom position of the groove. This distortion is caused by the relatively low pressure which induces a comparably low level of deformation. Therefore, the indentation depth does not reach the calculated depth. This results in minor deviation to the calculated roughness Rz but should be taken into account. A similar behavior is visible for $p_w = 14$ MPa. Here, the groove is also distorted. The peak height is a little higher in comparison to $p_w = 7$ MPa. Using the higher pressure of $p_w = 40$ MPa, the indentation depth as well as the peak height matches the analytically calculated surface in a high degree. This leads to the conclusion, that $Q_{def} > 7.28$ is necessary for the application of the analytical model to AISI1045 with 30 HRC. An exact value has to be determined experimentally.

Using a feed over $f = 0.3$ mm, the theoretical roughness increases in comparison to the experimentally generated roughness. The difference is higher when using lower pressures. Figure 10 depicts the surfaces after deep rolling using $f = 0.45$ mm to illustrate the differences of the surface topography using $p_w = 7$ MPa and 40 MPa. The surface generated by $p_w = 7$ MPa is comparable with the negative overlap described in the previous chapters: The initial turning induced peaks are not fully deformed. Resulting from the low degree of deformation, the grooves are not deep enough to reach the level of the analytically calculated surface. This combination results in a helical projection of the sphere’s geometry on the workpiece surface. Using $p_w = 40$ MPa, the surface is still fully deformed. The material is built up to a higher peak height. This results in a higher roughness and therefore a closer similarity to the analytic model.

It should however be noted that a deep rolling process with the goal of surface improvement is not a matter of interest for roughness values over $Rz = 4 \mu\text{m}$. Therefore, the region of interest can be changed to feed values under $f = 0.3$ mm in order to improve the visibility of the illustration.

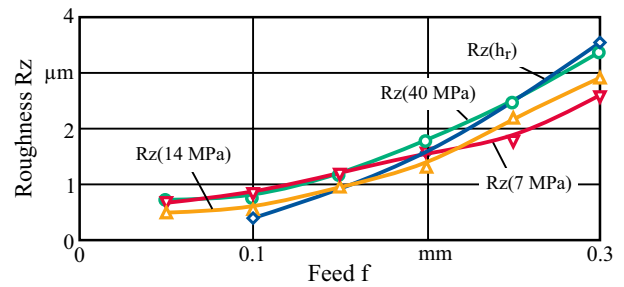
With this change of focus on lower feeds f and resulting roughness values Rz , the above described behavior can be confirmed, as visualized in Fig. 11. It should however be noted, that below $f = 0.1$ mm, the simple geometric model underestimates the roughness for $p_w = 7$ MPa and $p_w = 40$ MPa. The difference is lower for $p_w = 14$ MPa. Concerning these results, no clear influence of the deep rolling pressure p_w can be detected. Further investigations have to be performed in order to explain this behavior.

The application of the parameter variation leads to a similar surface progression on the other investigated materials. Machining the harder and therefore less plastic AISI4140 achieves a similar result, as indicated in Fig. 12. Here, the



Deep rolling	Tool:	ECOROLL HG6
Pressure: $p_w = \text{var.}$	Ball diameter: $d_b = 6.35$ mm	
Feed: $f = 0.45$ mm	Material: ceramic	
Overlap: $u = \text{var.}$	Workpiece:	AISI1045
		My/93280 @ IFW

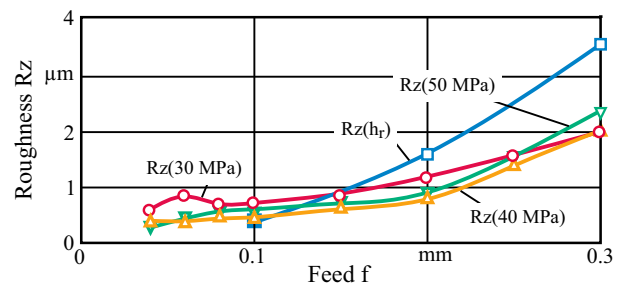
Fig. 10 Surfaces after deep rolling with alternating pressures p_w



Deep rolling	Tool:	ECOROLL HG6
Pressure: $p_w = \text{var.}$	Ball diameter: $d_b = 6.35$ mm	
Feed: $f = \text{var.}$	Material: ceramic	
Overlap: $u = \text{var.}$	Workpiece:	AISI1045
	Hardness: 302 HV1	
		My/93263_2a @ IFW

Fig. 11 Theoretical vs. experimental roughness for AISI1045 with focussed ROI

point of a differentiation between model and experimental surface is at $f = 0.2$ mm and therefore lower than for AISI1045. This result can be explained by the different plastic behavior of this harder material. Also visible is a higher accordance between model and experiment for $f > 0.1$ mm. In this range, the estimated roughness is higher for the lower deep rolling pressure of $p_w = 30$ MPa. This can be explained by the lower induced plastic deformation. It should also be mentioned that due to the above mentioned limitations of the compressor, the highest achieved ratio $Q_{def} = 6.59$ is lower than the lowest possible ratio for Al6082 ($Q_{def} = 6.66$). It can be concluded, that the model requires further adaptation for materials with high mechanical strength. Here, the approach of Bouzid et al. [7], where the plastic deformation is more carefully taken into account, could be applied. Another Option would be to increase the deep rolling pressure p_w to generate a higher Q_{def} . This approach is limited by the available compressor system.



Deep rolling	Tool:	ECOROLL HG6
Pressure: $p_w = \text{var.}$	Ball diameter: $d_b = 6.35$ mm	
Feed: $f = \text{var.}$	Material: ceramic	
Overlap: $u = \text{var.}$	Workpiece:	AISI4140
	Hardness: 515 HV1	
		My/93263b @ IFW

Fig. 12 Theoretical vs. experimental roughness for AISI4140

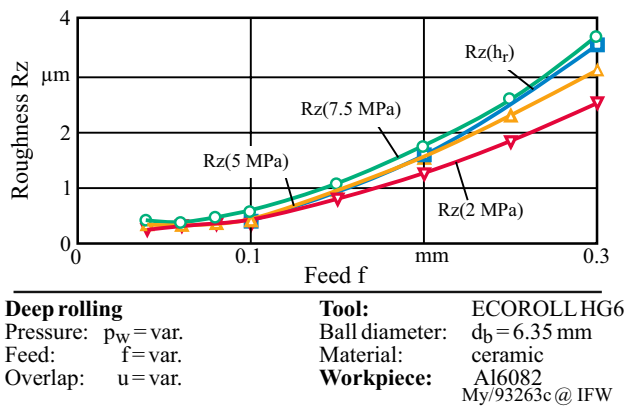


Fig. 13 Theoretical vs. experimental roughness for Al6082

To study the behavior of softer materials and compare the model for the Al6082, a repetition of the experiment was performed using pressures of $p_w = 2, 5$ and 7.5 MPa . As depicted in Fig. 13, the resulting surface topography is represented up to a feed of $f = 0.3 \text{ mm}$. The highest accordance of 93% is achieved using $p_w = 7.5 \text{ MPa}$ which results in $Q_{def} = 10.3$. With lower Q_{def} , the difference increases. Only small improvements of the resulting roughness are observed for every material below $f = 0.1 \text{ mm}$. Under the single-handed consideration of the roughness, smaller feeds are not recommended because they would increase process times in an industrial machining scenario. However, by reducing the feed, it is possible to further improve the residual stress state, especially regarding the residual stress-depth distribution as observed by Kämmler et al. [10]. A combined model for residual stresses and roughness could be used in industrial applications to optimize the relation between machining time and obtained result.

6 Conclusion and outlook

To predict the roughness of deep rolled surfaces for different materials, a geometry and deformation based model was designed following indications of the possibility to describe a two-dimensional tactile measurement by the intersection of spheres. This model was tested for a wide range of possible machining parameters and for three different materials. To describe the groove created by the deep rolling process according to this theory, a full deformation is necessary. The tendency for deformation can be described by Q_{def} , the quotient of the maximum Hertzian pressure p_{max} and the yield strength $R_{p0.2}$. Concluding from the experiments, $Q_{def} > 7$ was necessary. For the used setup, it was therefore possible to describe the surface for the softer materials Al6082 and AISI1045. The used compressor did not provide sufficient pressure p_w to achieve this criterion for quenched and tempered AISI4140. Another limit lies in the feed. The model

worked below feeds of $f < 0.3 \text{ mm}$. A further increase in feed rate would cause the maximum indentation width to be exceeded and complete deformation would not occur. Another point of focus should be the initial roughness state. In this paper, turning was used before the deep rolling process. These can also be influenced systematically by a variation of the feed f or the edge radius r_e . Further research could also apply this method to ground workpieces.

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Compliance with ethical standards

Conflict of interest The authors declare that they have no conflict of interest.

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